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Sulkhan Chavleishvili, Robert F. Engle, Stephan Fahr, Manfred Kremer, Simone Manganelli, Bernd Schwaab The risk management approach to macro-prudential policy

**Technical Papers** 



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### Abstract

Macro-prudential authorities need to assess medium-term downside risks to the real economy, caused by severe financial shocks. Before activating policy measures, they also need to consider their short-term negative impact. This gives rise to a risk management problem, an inter-temporal trade-off between expected growth and downside risk. Predictive distributions are estimated with structural quantile vector autoregressive models that relate economic growth to measures of financial stress and the financial cycle. An empirical study with euro area and U.S. data shows how to construct indicators of macro-prudential policy stance and to assess when interventions may be beneficial.

**Keywords:** Growth-at-risk, stress testing, quantile vector autoregression, financial conditions, macro-prudential policy.

JEL classification: G21, C33.

## Non-technical summary

The objective of macro-prudential policy is to make the financial system strong enough to withstand adverse shocks, taking advantage of good times to increase capital and liquidity buffers. According to this view, macro-prudential measures are recommended in case medium-term downside risks to the economy are deemed too severe. Such measures, however, can have short-term costs in terms of upside potential, or expected growth, of the economy. This paper proposes an econometric framework that allows macro-prudential authorities to optimally weigh the beneficial impact of their actions on future downside risks with the adverse impact of these actions on the upside potential of the economy.

There is a plethora of notions and techniques to measure downside risks. Yet, the question of how to make them operational for the conduct of macro-prudential policy has received much less attention. Recent research proposes to view a central bank's decision as a risk management problem, requiring the central bank to optimally balance downside and upside risks to price stability. This paper extends this idea to the macro-prudential problem, where the relevant authority sets its policy by optimally balancing the inter-temporal trade-off between expected growth and downside risks to the economy.

The paper uses a structural quantile vector autoregressive model (QVAR) to operationalize this methodological approach. The QVAR model allows us to quantify future risks to economic activity caused by elevated levels of financial stress as well as by economic vulnerability to shocks. We argue that our statistical framework inherits the best features from both the vector-autoregression (VAR) and quantile regression (QR) strands of literature. The VAR permits all endogenous variables to interact over time, allows us to be transparent about the identification of structural shocks, and can be used to simulate from the model and compare different counterfactual policy scenarios. QR allows the dynamic properties of the system to differ across quantiles, capturing potential asymmetries in the propagation of structural shocks.

The main body of the paper discusses the empirical findings for the euro area economy, using euro area data from 1988Q3 to 2018Q4. A companion web appendix shows that the results are qualitatively similar for the U.S. economy.

We focus on four empirical findings. First, a variable selection exercise suggests that central bank "intermediate target" variables, such as the financial cycle and money market interest rates,

interact closely with GDP growth and financial stress across all quantiles. We focus on the financial cycle because it can be influenced, at least to some extent, by macro-prudential policy instruments. In addition, our downside risk estimates are not particularly sensitive to the exclusion of short-term interest rates.

Second, the dynamic properties of the system differ significantly across quantiles. A formal Wald test rejects the parameter homogeneity restrictions implied by a linear VAR specification for our data at any reasonable confidence level. The QVAR is instead characterized by substantial asymmetries. In particular, a shock to financial stress shifts the left tail of future GDP towards more negative values, while leaving its conditional median and right tail approximately unaffected. The model-implied downside risk measures are strongly sensitive to the inclusion of financial variables.

Third, we find that the euro area economy is not equally resilient to the same sequence of adverse financial shocks at all times. The asymmetries uncovered in the data suggest that our QVAR model provides a natural environment to perform repeated model-based macro-prudential stress tests for the economy as a whole. Our model-based stress testing outcomes can be used as a quantitative yardstick to help calibrate the size of macro-prudential capital and liquidity buffers. Having multiple, complementary approaches available for this purpose may help overcome a potential "inactivity-bias," according to which few jurisdictions have set their counter-cyclical capital buffers to above-zero levels from the buffer's inception in 2014 to late 2019.

Fourth, the QVAR estimates can provide a metric to assess whether the macro-prudential stance is too tight or too loose. To counteract the feedback and the asymmetries captured in the estimated structural QVAR, we argue that macro-prudential policy should act in a counter-cyclical fashion by releasing buffers when downside risk is exceptionally high and increasing them when downside risk is low. Welfare calculations from stabilizing the financial cycle can be based on a suitably chosen objective function. The associated welfare gains can be positive or negative, and are most positive in exuberant times when the financial cycle is above its conditional median.

## **1** Introduction

The Stoic philosopher Seneca once observed that "When pleasures have corrupted both mind and body, nothing seems tolerable – not because the suffering is hard, but because the sufferer is soft."<sup>1</sup> The quote nicely encapsulates a common view of macro-prudential policy: Make the financial system strong (hard) enough to withstand adverse shocks, taking advantage of good times to build up buffers and increase fortitude. According to this view, the activation of macro-prudential measures is recommended in case medium-term downside risks to the economy are deemed too severe. Such measures, however, are not necessarily without costs to the upside potential, or expected growth, of the economy. This paper proposes an econometric framework based on which macro-prudential authorities can optimally weigh the beneficial impact of their actions on future downside risks with the adverse impact of these actions on the upside potential of the economy.

There is a plethora of notions and techniques to measure downside risk. Yet, the question of how to make them operational for the conduct of macro-prudential policy has received much less attention. Greenspan (2003, p. 3), Cecchetti (2006), and Kilian and Manganelli (2008) propose to view a central bank's decision as a risk management problem, requiring the central bank to optimally balance downside and upside risks to price stability. This paper extends their idea to the macro-prudential problem, where the relevant authority sets its policy by optimally balancing the inter-temporal trade-off between expected growth and downside risk to the economy. Related methodological approaches have recently been advocated by Carney (2020), Suarez (2021), and, from a general equilibrium perspective, Mendicino et al. (2018) and Caballero and Simsek (2020).

This paper uses a quantile vector autoregressive model (QVAR) to operationalize our risk management idea. QVAR was first proposed in unpublished work by Cecchetti and Li (2008). Independent work by White et al. (2015), Chavleishvili and Manganelli (2019) and Montes-Rojas (2019) has formalized the econometric model. These contributions fit into the broader literature on multivariate quantile regression, which is an active area of research (see, for instance, Wei (2008) or Carlier et al. (2016) and the references therein).

<sup>&</sup>lt;sup>1</sup>Seneca, De Ira, Liber II, XXV, 3.

We show how QVAR provides the ideal econometric tool to address many of the policy issues faced by macro-prudential authorities. It can be used to obtain: estimates of financial stability risks which are easy to communicate, a variable selection procedure for a multivariate model of downside risk, a stress testing assessment of the vulnerability of the financial system, and a measure of macro-prudential policy stance. The main body of the paper discusses the empirical findings for the euro area economy. A companion web appendix shows that the results are qualitatively similar for the U.S. economy.

A rapidly growing body of research has examined downside risk in macroeconomic outcomes. Most of this work has focused on the risk of significant declines in gross domestic product (GDP), brought about by a deterioration of financial conditions. In particular, growth-at-risk (GaR), the, say, 5% quantile of a predictive GDP distribution, has emerged as a popular measure of downside risk; see e.g. Adrian et al. (2019), Prasad et al. (2019), and Caldara et al. (2019). Both the International Monetary Fund (IMF) as well as the European Central Bank (ECB) now routinely publish GaR estimates for major world economies; see IMF (2017) and ECB (2019). These developments have motivated a proliferation of modeling frameworks to assess the severity of extreme events associated with key economic variables, including single-equation quantile regression (QR) models (Adrian et al. (2019)), panel QR models (Adrian et al. (2018), Brandao-Marques et al. (2020)), panel-GARCH models (Brownlees and Souza (2020)), fully non-parametric kernel regression models (Adrian et al. (2020)), combined linear vector autoregressive (VAR) and singleequation QR models (Duprey and Ueberfeldt (2020)), nonlinear Bayesian VAR models (Caldara et al. (2019), Carriero et al. (2020)), and quantile VAR models (Chavleishvili and Manganelli (2019)). De Santis and van der Veken (2020) show that even if a recession is due to an unforseen real shock (as the recent Covid-19 recession) financial variables can still help policy makers by providing timely warnings about the severity of the crisis and the macroeconomic risks involved. Plagborg-Moller et al. (2020) provide a critical review of this literature.

This paper embeds the insights from this large empirical literature on downside risk into a macro econometric model that can be used to produce structural forecast distributions, taking into

account the strong asymmetries that characterize macro-financial interactions. The QVAR model allows us to quantify future risks to economic activity caused by elevated levels of financial stress as well as by economic vulnerability to shocks. We argue that our framework inherits the best features from both the VAR and QR strands of literature. The VAR permits all endogenous variables to interact over time, allows us to be transparent about the identification of structural shocks, and can be used to simulate from the model and compare different counterfactual policy scenarios. QR allows the dynamic properties of the system to differ across quantiles, capturing potential asymmetries in the propagation of structural shocks. As a welcome by-product, QR parameter estimates are less sensitive to outliers when compared to their least squares counterparts. This robustness feature can become relevant when financial variables are included in the model and the financial system and the economy face abrupt and large changes. Succinctly put, our QVAR model relates to the single-equation QR approach of Adrian et al. (2019) as the VAR model of Sims (1980) relates to the straightforward single-equation autoregressive approaches of e.g. Koyck (1954) and Almon (1965).

To relate to the problem faced by macro-prudential authorities, we include measures of financial stress and medium-term vulnerabilities alongside GDP growth in our baseline model. Indicators of financial stress serve as a macro-finance amplification mechanism that characterise financial crises. Measures of vulnerabilities represent intermediate target variables on which policy makers can act by activating their policy tools. The three-variable setup reflects the consideration that financial stability is of concern to policy makers if it is triggered by an impairment of the financial system and has real economic consequences, e.g. in terms of future employment, consumption, or overall economic activity.<sup>2</sup> Financial stress is proxied by the ECB's Composite Indicator of Systemic Stress (CISS; see Hollo et al. (2012)), while medium-term vulnerabilities are proxied by Schüler et al. (2020) real-time broad financial cycle indicator. Financial stress, the financial cycle,

<sup>&</sup>lt;sup>2</sup>The ECB definition of financial stability refers to "the risk that the provision of necessary financial products and services by the financial system will be impaired to a point where economic growth and welfare may be materially affected;" see ECB (2019). Similarly, the Financial Stability Board, International Monetary Fund, and the Bank for International Settlements define systemic risk as a "risk of disruption to financial services that is (i) caused by an impairment of all or parts of the financial system, and (ii) has the potential to have serious negative consequences for the real economy;" see FSB (2009).

and GDP growth can interact freely in our preferred model specification, and can do so to different extents at different quantiles.

The empirical part of this paper applies our statistical model to both euro area and U.S. data. The paper focuses on euro area data between 1988Q3 and 2018Q4,<sup>3</sup> and analogous tables and figures based on U.S. data between 1973Q1 and 2018Q4 are discussed in the web appendix. Our main findings are remarkably similar across the euro area and U.S. samples.

We focus on four empirical findings. First, a variable selection exercise suggests that central bank "intermediate target" variables, such as the financial cycle and (de-trended) money market interest rates, interact closely with GDP growth and financial stress across all quantiles. Other variables, such as the term spread may also play a role, particularly for U.S. data, but are not ranked as highly by model selection criteria. We focus on the financial cycle because it can be influenced, at least to some extent, by macro-prudential (and monetary) policy instruments (Cerutti et al. (2017)). Our downside risk estimates are not particularly sensitive to the exclusion of short-term interest rates; we therefore use the more parsimonious trivariate model specification for most of our results.

Second, the dynamic properties of the system differ significantly across quantiles. A formal Wald test rejects the pooling, or parameter homogeneity, restrictions implied by a linear VAR specification for our data at any reasonable confidence level. The QVAR is instead characterized by substantial asymmetries. In particular, a shock to financial stress shifts the left tail of future GDP towards more negative values, while leaving its conditional median and right tail approximately unaffected. As in Adrian et al. (2019), macro-financial interactions imply that the upper quantiles of predictive GDP growth distribution are less volatile than its lower quantiles. Our model-implied downside risk measures are strongly sensitive to the inclusion of financial variables. Not only does downside risk associated with the global financial crisis between 2008 and 2009 decline much later, and to a lesser extent, when financial stress is missing, but in addition the downside risk associated with the 2010–2012 euro area sovereign debt crisis is missed almost entirely when financial stress

<sup>&</sup>lt;sup>3</sup>Counterfactual data preceding the formation of the euro area (pre-1999) is obtained from an internal ECB database.

is not included in the model.

Third, we find that the euro area economy is not equally resilient to the same sequence of adverse financial shocks at all times. The asymmetries uncovered in the data suggest that our QVAR model provides a natural environment to perform repeated model-based macro-prudential stress tests for the economy as a whole. We here understand stress testing as a forecast of what would happen to all variables in the system should it be subjected to a fixed sequence of adverse shocks. We find that downside risk conditional on future adverse real and financial shocks spikes during crises. Our model-based stress testing outcomes can be used as a quantitative yardstick to help calibrate the size of macro-prudential capital and liquidity buffers.

Fourth, our risk management framework and its underlying econometric model can be used to guide financial stability policies. In QVAR-based stress tests, the impact of a shock to financial conditions (stress) depends not only on its initial severity, but also on the endogenous, asymmetric responses of all other variables in the system. Allowing for such feedback and asymmetries is crucial when subjecting the system to a sequence of tail shocks. To counteract the feedback and the asymmetries, we argue that macro-prudential policy should act in a counter-cyclical fashion by releasing buffers when downside risk is exceptionally high, and increasing them when downside risk is exceptionally low (Van der Ghote (2021)). Welfare calculations from stabilizing the financial cycle can be based on a suitably chosen objective function. The associated welfare gains can be positive or negative, and are most positive in exuberant times when the financial cycle is above its conditional median. The QVAR estimates therefore provide a metric to assess whether the macro-prudential stance is too tight or too loose. Model-based stress testing and scenario analysis can complement early warning indicators such as the credit-to-GDP-ratio gap that has traditionally informed the calibration of the counter-cyclical capital buffer. Having complementary approaches available may help overcome a potential "inactivity-bias," according to which few jurisdictions have set their counter-cyclical capital buffers to above-zero levels from the buffer's inception in 2014 to late 2019.<sup>4</sup>

<sup>&</sup>lt;sup>4</sup>At the end of 2018, 19 out of 28 European Union countries, and 15 out of 19 euro area countries, had countercyclical capital buffers set at zero; see Web Appendix A for details.

We proceed as follows. Section 2 defines our downside risk measures, introduces the risk management framework, and presents the statistical model. Section 3 describes our data. Section 4 applies the model to euro area and U.S. data. Section 5 concludes. A web appendix provides further technical and empirical results.

## 2 The risk management framework

This section starts by introducing measures of downside risk borrowed from the financial risk management literature. Next, it shortly summarizes the QVAR model and shows how it can be used for forecasting, for semi-parametric risk measurement and for counterfactual analysis. It ends by pulling these elements together into an encompassing risk management framework.

## 2.1 Measures of downside risk and upside potential

We define three measures of downside risk, which are well-known in the risk management literature. Each measure is of interest in different settings.

## 2.1.1 Growth-at-risk

Our first measure of adverse impact is *growth-at-risk* ( $\text{GaR}_{t,t+h}^{\gamma}$ ) at confidence level  $\gamma \in (0,1)$ , defined implicitly by the probability

$$\mathbb{P}\left[y_{t+h} \le \operatorname{GaR}_{t,t+h}^{\gamma} | \mathcal{F}_{1t}\right] = \gamma,\tag{1}$$

where  $y_t$  denotes the quarterly annualized real GDP growth rate between time t - 1 and t, and h = 1, ..., H denotes a certain prediction horizon. The information set  $\mathcal{F}_{1t}$  contains all data known at time t; see Section 2.2 below. In words,  $\operatorname{GaR}_{t,t+h}^{\gamma}$  is implicitly defined by the time t probability of quarterly annualized output growth at t + h falling below  $\operatorname{GaR}_{t,t+h}^{\gamma}$ , which by definition is set equal to  $\gamma$ .

## 2.1.2 Growth shortfall

Our second measure of adverse real economic impact is growth shortfall (GS), defined as

$$\mathbf{GS}_{t,t+h}^{\tau} = \int_{-\infty}^{\tau} y_{t+h} dF_{t,t+h}(y_{t+h})$$
$$= \mathbb{E}\left[y_{t+h} | y_{t+h} < \tau, \mathcal{F}_{1t}\right] \times \mathbb{P}\left[y_{t+h} < \tau | \mathcal{F}_{1t}\right], \tag{2}$$

where  $F_{t,t+h}$  is a time-*t* conditional cumulative distribution function (cdf),  $\mathbb{E}[\cdot|\mathcal{F}_{1t}]$  denotes a time*t* conditional expectation, and the threshold  $\tau \in \mathbb{R}$  could be set to a low conditional quantile, say  $\tau = \text{GaR}_{t,t+h}^{\gamma}$ . If so, then the first factor in (2) coincides with the familiar notion of expected shortfall; see e.g. McNeil et al. (2005, Ch. 2). Alternatively, it could be set to a certain unconditional quantile, or be set to zero.

If  $\tau = 0$ , GS can be factored into two intuitive terms: the expected loss conditional on a contraction, and the probability of experiencing a contraction.<sup>5</sup> While both components can be studied separately and can be of interest in their own right, such as in stress test or macroeconomic modeling, GS summarizes them tractably into one metric and is easily obtained from a QVAR model. When  $\tau = 0$ , GS corresponds to the economic question: what is the time *t*-expected contraction of the economy at time t + h?

### 2.1.3 Average growth shortfall

Our final measure of adverse real economic impact is the *average future growth shortfall* (AGS) between t + 1 and t + H, defined as

$$AGS_{t,t+1:t+H}^{\tau} = H^{-1} \sum_{h=1}^{H} GS_{t,t+h}^{\tau}.$$
(3)

If  $\tau = 0$ , then the AGS corresponds to the question: what is the average future expected contraction of the economy between t + 1 and t + H. Since it is an average of future GS, AGS retains all the

<sup>5</sup>To see this, note that 
$$\mathbb{E}\left[y_{t+h}|y_{t+h} < \tau, \mathcal{F}_{1t}\right] \equiv \frac{\int_{-\infty}^{\infty} y_{t+h} \cdot \mathbf{1}\{y_{t+h} < \tau\} dF_{t,t+h}(y_{t+h})}{\int_{-\infty}^{\infty} \mathbf{1}\{y_{t+h} < \tau\} dF_{t,t+h}(y_{t+h})} = \frac{\int_{-\infty}^{\tau} y_{t+h} dF_{t,t+h}(y_{t+h})}{\mathbb{P}[y_{t+h} < \tau|\mathcal{F}_{1t}]}$$

statistical properties of GS.

All above risk measures are economically intuitive and straightforward to communicate. Risk measures (2) and (3), however, have theoretical and practical advantages over (1). First, expected shortfall-based measures are coherent risk measures, while any single quantile in isolation is not (Artzner et al. (1999)). For example, GS contributions are sub-additive, while GaR contributions are not. This feature is desirable if one, for instance, wants to study sector contributions to aggregate GDP at risk. Second, while all above risk measures (1) – (3) can take into account the asymmetric impact of financial variables on the economy, only (2) and (3) take into account the entire left tail.

When considering financial stability policies aimed at containing downside risk, then the expected growth rate of the economy, as well as the upper quantiles of future GDP growth, should not be unduly affected. For setting up the risk management framework later in section 2.3, we consider two measures of upside potential that are symmetric to the measures of downside risk just defined.

#### 2.1.4 Growth longrise

We define the growth longrise<sup>6</sup> (GL) as the complement to GS,

$$GL_{t,t+h}^{\tau} = \int_{\tau}^{\infty} y_{t+h} dF_{t,t+h}(y_{t+h})$$
$$= \mathbb{E} \left[ y_{t+h} | y_{t+h} > \tau, \mathcal{F}_{1t} \right] \times \mathbb{P} \left[ y_{t+h} > \tau | \mathcal{F}_{1t} \right].$$
(4)

If  $\tau = 0$ , then (4) corresponds to the question: what is the time-t expected expansion of the economy between t + h - 1 and t + h? Similarly to GS, the growth longrise (4) captures the expected growth given an expansion, and the conditional probability of experiencing an expansion.

<sup>&</sup>lt;sup>6</sup>The term longrise was coined by Adrian et al. (2019) as the antonym to shortfall.

## 2.1.5 Average growth longrise

Analogously to (3), we also define the *average growth longrise* (AGL) between t + 1 and t + H as

$$AGL_{t,t+1:t+H}^{\tau} = H^{-1} \sum_{h=1}^{H} GL_{t,t+h}^{\tau}.$$
(5)

Given the complementarity between GS and GL, their sum equals the expected growth rate of the economy between t + h - 1 and t + h,

$$\mathbb{E}\left[y_{t+h}|\mathcal{F}_{1t}\right] = \int_{-\infty}^{\infty} y_{t+h} dF_{t,t+h}(y_{t+h})$$
$$= \int_{-\infty}^{\tau} y_{t+h} dF_{t,t+h}(y_{t+h}) + \int_{\tau}^{\infty} y_{t+h} dF_{t,t+h}(y_{t+h})$$
$$= \mathbf{GS}_{t,t+h}^{\tau} + \mathbf{GL}_{t,t+h}^{\tau}.$$

Furthermore, let  $\bar{y}_{t,t+1:t+H} = H^{-1} \sum_{h=1}^{H} y_{t,t+h}$  be the average future economic growth rate between t + 1 and t + H. Since (2) and (4) are linear, the expected future growth rate of the economy between t + 1 and t + H is  $\mathbb{E}[\bar{y}_{t,t+1:t+H}|\mathcal{F}_{1t}] = AGS_{t,t+1:t+H}^{\tau} + AGL_{t,t+1:t+H}^{\tau}$ . As a result, expected average future growth can be read off any figure reporting  $AGS_{t,t+1:t+H}^{\tau}$  and  $AGL_{t,t+1:t+H}^{\tau}$  by adding the two lines.

## 2.2 Quantile vector autoregression

This section provides a concise exposition of the structural quantile vector autoregressive (QVAR) model of Chavleishvili and Manganelli (2019) and shows how it can be used to obtain semiparametric estimates of (1) - (5).<sup>7</sup> The structural identification is obtained by imposing triangular restrictions and can be thought of as a macro-econometric application of the approach proposed by Wei (2008). Intuitively, the QVAR model provides the forecast of the quantiles of the distribution of the endogenous variables at any period ahead. The quantile forecasts can be treated as the

<sup>&</sup>lt;sup>7</sup>See also Montes-Rojas (2019) and Ruzicka (2020) for related work on QVAR parameter and quantile impulse response function estimation.

equivalent of an empirical distribution and can therefore be used to approximate the risk quantities discussed in the previous section. Furthermore, since we attach a structural interpretation to the model, the structural shocks can be recovered and used to perform counterfactual exercises, as one would do with a standard VAR.

### 2.2.1 The model

We observe a series of random variables  $\{\tilde{x}_t : t = 1, ..., T\}$ , where  $\tilde{x}_t \in \mathbb{R}^n$  is an *n*-vector with  $i^{th}$  element denoted by  $\tilde{x}_{it}$  for i = 1, ..., n and  $n \in \mathbb{N}$ . For any arbitrary but fixed quantile  $\gamma$ , the QVAR model of order 1 is given by

$$\tilde{x}_{t+1} = \omega^{\gamma} + A_0^{\gamma} \tilde{x}_{t+1} + A_1^{\gamma} \tilde{x}_t + \epsilon_{t+1}^{\gamma}$$
(6)

$$\mathbb{P}(\epsilon_{i,t+1}^{\gamma} < 0 | \mathcal{F}_{it}) = \gamma, \quad \text{for } i = 1, \dots, n,$$
(7)

where the vector of structural quantile residuals is given by  $\epsilon_t^{\gamma} \equiv [\epsilon_{1t}^{\gamma}, \dots, \epsilon_{nt}^{\gamma}]'$ . Recursive identification is achieved by restricting the  $[n \times n]$  matrix  $A_0^{\gamma}$  to be lower triangular with zeros along the main diagonal. The presence of contemporaneous dependent variables on the right-hand side of (6) requires us to be precise about the available information at any time and for each variable. We work with a recursive information set that increases one scalar observation at a time,

$$\mathcal{F}_{1t} = \{\tilde{x}_t, \tilde{x}_{t-1}, \ldots\}$$
(8)

$$\mathcal{F}_{it} = \{ \tilde{x}_{i-1,t+1}, \mathcal{F}_{i-1,t} \} \text{ for } i \in \{2, \dots, n\}.$$
(9)

In words,  $\mathcal{F}_{1t}$  contains only variables observed up to time t. The information sets  $\mathcal{F}_{it}$  for i > 1 contain increasingly more information about variables observed at  $t + 1.^8$ 

We may wish to consider multiple quantiles of multiple variables at the same time. To do this in a compact way, we consider p distinct quantiles  $0 < \gamma_1 < \cdots < \gamma_p < 1$ , for  $p \in \mathbb{N}$ , not necessarily equidistant. In addition, we let  $x_t \equiv [\iota_p \otimes \tilde{x}_t]$  denote the vector stacking p times the dependent

<sup>&</sup>lt;sup>8</sup>For a similar incremental conditioning approach in a different setting see e.g. Koopman and Durbin (2000).

variables  $\tilde{x}_t$ , where  $\iota_p$  is a *p*-vector of ones. The stacked QVAR model of order 1 is then given by

$$x_{t+1} = \omega + A_0 x_{t+1} + A_1 x_t + \epsilon_{t+1} \tag{10}$$

$$\mathbb{P}(\epsilon_{i,t+1}^{\gamma_j} < 0 | \mathcal{F}_{it}) = \gamma_j, \quad \text{for } i = 1, \dots, n, \quad j = 1, \dots, p$$
(11)

where the vector of structural quantile residuals is given by  $\epsilon_t \equiv [\epsilon_{1t}^{\gamma_1}, \dots, \epsilon_{nt}^{\gamma_1}, \dots, \epsilon_{nt}^{\gamma_p}, \dots, \epsilon_{nt}^{\gamma_p}]'$ . The  $[np \times np]$  matrices  $A_0$  and  $A_1$  are block diagonal to avoid trivial multicollinearity problems. The model (10) – (11) is essentially a convenient way to stack p quantile-specific QVAR models (6) – (7).

An explicit example may be instructive. While the baseline empirical model in Section 4 considers three variables, we here develop intuition based on a simpler bivariate model for the data vector  $\tilde{x}_t = (y_t, s_t)'$ , where  $y_t$  is the quarterly annualized real GDP growth between t - 1 and t, and  $s_t$  is a coincident indicator of systemic financial stress. Let us consider p = 2 quantiles for simplicity, 0.10 and 0.90. The system (10) – (11) can then be written as

$$\begin{bmatrix} y_{t+1} \\ s_{t+1} \\ s_{t+1} \\ s_{t+1} \end{bmatrix} = \begin{bmatrix} \omega_y^{\cdot 1} \\ \omega_y^{\cdot 1} \\ \omega_y^{\cdot 9} \\ \omega_s^{\cdot 9} \end{bmatrix} + \begin{bmatrix} 0 & 0 & 0 & 0 \\ a_{021}^{\cdot 1} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & a_{021}^{\cdot 9} & 0 \end{bmatrix} \begin{bmatrix} y_{t+1} \\ s_{t+1} \\ y_{t+1} \\ s_{t+1} \end{bmatrix} + \begin{bmatrix} a_{t+1}^{\cdot 1} & a_{t+1}^{\cdot 1} \\ a_{11}^{\cdot 1} & a_{12}^{\cdot 1} \\ a_{21}^{\cdot 1} & a_{22}^{\cdot 1} & 0 & 0 \\ a_{21}^{\cdot 1} & a_{22}^{\cdot 1} & 0 & 0 \\ 0 & 0 & a_{11}^{\cdot 9} & a_{12}^{\cdot 9} \\ 0 & 0 & a_{21}^{\cdot 9} & a_{22}^{\cdot 9} \end{bmatrix} \begin{bmatrix} y_t \\ s_t \\ y_t \\ s_t \end{bmatrix} + \begin{bmatrix} \epsilon_{y,t+1}^{\cdot 1} \\ \epsilon_{s,t+1}^{\cdot 1} \\ \epsilon_{y,t+1}^{\cdot 9} \\ \epsilon_{y,t+1}^{\cdot 9} \\ \epsilon_{y,t+1}^{\cdot 9} \end{bmatrix}$$
(12)

Here, the ordering of the observations in (12) reflects the assumption that the financial stress variable  $s_t$  can react contemporaneously to macroeconomic shocks, while real output growth  $y_t$  can react to financial shocks only with a lag. Such triangular identification assumptions are standard in the empirical literature; see e.g. Christiano et al. (1999), Kilian (2009), and Gilchrist and Zakrajsek (2012), among many others.

#### 2.2.2 Forecasting

This section explains how forecasts can be generated from the stacked QVAR model (10) – (11) without invoking parametric assumptions on  $\epsilon_{t+1}$ .

It is helpful to introduce the conditional quantile operator  $Q_{it}^{\gamma_j}(x_{k,t+1})$ , where  $x_{k,t+1}$  is the k-th element of  $x_{t+1}$ , k = 1, ..., np. Given information set  $\mathcal{F}_{it}$ , the operator is implicitly defined by

$$\mathbb{P}\left(x_{k,t+1} < Q_{it}^{\gamma_j}(x_{k,t+1}) | \mathcal{F}_{it}\right) = \gamma_j, \quad \text{for } j = 1, \dots, p.$$

In words,  $Q_{it}^{\gamma_j}(x_{k,t+1})$  returns the  $\gamma_j$  quantile of random variable  $x_{k,t+1}$  conditional on  $\mathcal{F}_{it}$ . The element  $x_{k,t+1}$  is random because it depends on its own shock at time t + 1, but also on shocks to earlier elements  $x_{1,t+1}, \ldots, x_{k-1,t+1}$ .

To build intuition first, let us return to the simple bivariate example (12) with n = p = 2. Let's assume we are interested in forecasting, say, the 0.9 quantile of the financial stress variable  $s_{t+1}$ . The fourth equation of (12), corresponding to the 0.9 quantile of  $s_{t+1}$ , is

$$s_{t+1} = \omega_s^{.9} + a_{021}^{.9} [\omega_y^{.9} + a_{11}^{.9} y_t + a_{12}^{.9} s_t + \epsilon_{y,t+1}^{.9}] + a_{21}^{.9} y_t + a_{22}^{.9} s_t + \epsilon_{s,t+1}^{.9}$$

$$= \omega_s^{.9} + a_{021}^{.9} \omega_y^{.9} + (a_{021}^{.9} a_{11}^{.9} + a_{21}^{.9}) y_1 + (a_{021}^{.9} a_{12}^{.9} + a_{22}^{.9}) s_t + a_{021}^{.9} \epsilon_{y,t+1}^{.9} + \epsilon_{s,t+1}^{.9}$$

$$= q_{st}^{.9} + a_{021}^{.9} \epsilon_{y,t+1}^{.9} + \epsilon_{s,t+1}^{.9}$$
(13)

where  $q_{st}^{.9} \equiv \omega_s^{.9} + a_{021}^{.9} \omega_y^{.9} + (a_{021}^{.9} a_{11}^{.9} + a_{21}^{.9}) y_t + (a_{021}^{.9} a_{12}^{.9} + a_{22}^{.9}) s_t$  depends only on deterministic parameters to be estimated and variables observed at time t. We note that  $Q_{st}^{.9}(\epsilon_{s,t+1}^{.9}) = 0$  because of the identifying restriction (11), stating  $\mathbb{P}\left(\epsilon_{s,t+1}^{.9} < 0 | \mathcal{F}_{st}\right) = 0.9$  when  $\mathcal{F}_{st} = \{y_{t+1}, y_t, s_t, \ldots\}$ . In addition,  $q_{st}^{.9} + a_{021}^{.9} \epsilon_{y,t+1}^{.9} | \mathcal{F}_{st}$  is non-random. As a result,  $Q_{st}^{.9}(s_{t+1}) = q_{st}^{.9} + a_{021}^{.9} \epsilon_{y,t+1}^{.9}$  is still a random variable at time t. To eliminate this randomness, we keep on taking quantiles. Using the identifying restriction (11) again,  $Q_{yt}^{.9}(\epsilon_{y,t+1}^{.9}) = 0$  yields  $Q_{yt}^{.9}(Q_{st}^{.9}(s_{t+1})) = q_{st}^{.9}$ . As a result,  $q_{st}^{.9}$  is our sought-after forecast of the 0.9 quantile of  $s_{t+1}$ , and is easily computed. This approach of iterated quantiles can be repeated for any potentially remaining variables in  $x_{t+1}$ . Following that, the approach can be repeated for future variables in  $x_{t+h}$  for h > 1.9

The above reasoning can be formalized. The scalar operators  $Q_{it}^{\gamma_j}(x_{k,t+1})$  can be combined into a vector version, with quantile operators nesting each other up to n times. The vector operators can again be sequentially combined, up to H times. In the end, the  $[np \times 1]$ -vector of quantile forecasts at time t associated with process (10), for  $h = 1, \ldots, H$ , can be obtained quite straightforwardly as

$$\hat{x}_{t+h} = \sum_{j=0}^{h-1} B^j \nu + B^h x_t,$$
(14)

where  $\nu = (I_{np} - A_0)^{-1} \omega$  and  $B = (I_{np} - A_0)^{-1} A_1$ . It is easily verified that  $\hat{x}_{4,t+1}$  (i.e., the fourth element of  $\hat{x}_{t+1}$ , obtained using (14)) coincides with  $q_{st}^{.9}$  as defined below (13).

#### 2.2.3 Semi-parametric risk measurement

This section explains how we obtain the time-*t* downside risk measures introduced in Section 2.1 from our semi-parametric structural QVAR model (10) - (11) using simulation methods. To this end we rely on a growing literature on simulation methods for quantile regression; see e.g. Hahn (1995) and Koenker (2005, Ch. 2.6).

When we defined the structural QVAR model for an arbitrary quantile  $\gamma$  as (6) – (7), and insisted that the model holds for all  $\gamma \in (0, 1)$ , we effectively specified a complete stochastic mechanism for generating the one-step ahead variable  $\tilde{x}_{t+1}$  conditional on time-*t* information and deterministic parameters. Recall that any scalar response variable  $\tilde{x}_{i,t+1}$ ,  $i = 1, \ldots, n$ , with conditional cdf  $F_{i,t,t+1}$ , can be simulated by generating a uniform random variable  $u_{i,t+1} \sim U[0, 1]$ , and then setting  $\tilde{x}_{i,t+1} = F_{i,t,t+1}^{-1}(u_{i,t+1})$ . Thus, in model (6) – (7),  $\tilde{x}_{i,t+1}$  can be simulated setting  $\tilde{x}_{i,t+1} = \omega_i^{u_{i,t+1}} + A_{0,i}^{u_{i,t+1}} \tilde{x}_{t+1} + A_{1,i}^{u_{i,t+1}} \tilde{x}_{t}$ , where  $\omega_i^{(\cdot)}$ ,  $A_{0,i}^{(\cdot)}$ , and  $A_{1,i}^{(\cdot)}$  denote the *i*-th row of  $\omega^{\gamma}$ ,  $A_0^{\gamma}$ ,

<sup>&</sup>lt;sup>9</sup> This example implicitly assumes that  $a_{021}^{.9}$  is positive. If not, then the 0.9 conditional quantile and the 0.1 conditional quantile cross. This is because, when  $a_{021}^{.9} < 0$ , then  $\mathbb{P}\left(a_{021}^{.9}\epsilon_{y,t+1}^{.9} < 0\right) = \mathbb{P}\left(\epsilon_{y,t+1}^{.9} > 0\right) = 1 - \mathbb{P}\left(\epsilon_{y,t+1}^{.9} < 0\right) = 1 - \mathbb{P}\left(\epsilon_{y,t+1}^{.9} < 0\right) = 1 - 0.9 = 0.1$ . If this happens we reorder (relabel) the quantiles accordingly.

and  $A_1^{\gamma}$ , respectively, evaluated at  $\gamma = u_{i,t+1}$ .<sup>10</sup> This procedure allows us to generate the  $\tilde{x}_{i,t+h}$ , recursively, for i = 1, ..., n and h = 1, ..., H, conditional on the relevant information sets.

We sketch our simulation algorithm here, and refer to Web Appendix B.4 for details. Let t = 1, ..., T denote any time in our sample. With *n* variables, *p* quantiles and *H* steps ahead, there are  $p^{nH}$  possible paths, a number which quickly becomes computationally unmanageable. We resort instead to simulation, by randomly generating *S* potential future paths for all *n* variables in  $\tilde{x}_{i,t+h}$ , h = 1, ..., H quarters ahead.<sup>11</sup> The simulations are based on inverse cdf-sampling by drawing S = 10,000 sequences of  $nH = 3 \times 8 = 24$  uniform random variables with support  $[\gamma_1, ..., \gamma_p]$ , and use the one-step-ahead recursion (6). At each t + h, we calculate  $GS_{t,t+h}^{\tau}$  and  $GL_{t,t+h}^{\tau}$  by evaluating the sample analogues of (2) and (4). At the end, we average across *H* to obtain downside risk measures  $AGS_{t,t+1:t+h}^{\tau}$  and  $AGL_{t,t+1:t+h}^{\tau}$ ; see (3) and (5).<sup>12</sup>

## 2.2.4 Counterfactual scenarios

Web Appendix B.5 explains in detail how counterfactual scenarios can be obtained from the QVAR model (10) – (11). Rather than moving through the complete tree of potential future values of  $\tilde{x}_{t+h}$  at random, as explained in Section 2.2.3, we then consider only one path in isolation. Such a path can be thought of as a 'counterfactual scenario,' or model-based thought experiment that conditions on an arbitrary but fixed sequence of future shocks. We use such counterfactual scenarios when considering a market-based stress test in Section 4.3, and when studying the benefits vs. cost from tightening macro-prudential policy stance in Sections 4.4.

<sup>&</sup>lt;sup>10</sup>Recall that  $A_0$  is lower triangular.

<sup>&</sup>lt;sup>11</sup>The simulation approach is no panacea, as S still needs to be chosen large enough to sufficiently explore the tree. Our risk estimates presented in Section 4 are insensitive to the initial random seed and to variations in the number of simulations.

<sup>&</sup>lt;sup>12</sup>Rather than re-estimating the model parameters within each simulation and for each variable using  $\gamma_i = u_{i,t+h}$ , it is computationally advantageous to discretize the support of the standard uniform random variable with an appropriately chosen grid  $0 < \gamma_1 < \ldots < \gamma_p < 1$ , and to estimate all parameters once and for all in the beginning based on the full sample. We then use the parameter estimates associated with the closest selected quantile in any simulation. We use p = 20 grid-points for this purpose,  $0 < 0.025, 0.075, \ldots, 0.925, 0.975 < 1$ , each at the midpoint of 1/20th of the unit interval. These grid-points are symmetric around the median, and yield equi-probable simulation paths. Crossing quantiles (see footnote 9) are not an issue since we move through the tree at random. Our downside risk estimates reported in Section 4.2 are robust to increasing the number of grid-points, and to interpolating parameter estimates between quantiles.

## 2.3 Putting it all together in a risk management framework

A key question for a policy maker is to what extent a policy intervention reduces downside risk to the economy and what risk it imposes in terms of reduced growth. In other words, how is a policy maker to assess the change in forecast distributions triggered by its actions? The risk management framework answers this question by requiring the policy maker to be explicit about the trade-off between downside risk and upside potential. It is equivalent to requiring the decision maker to provide a loss function, and setting the policy variables to levels that minimize such a loss. We believe that framing the problem in terms of risk management facilitates the elicitation of the preferences of the policy maker and the communication of the policy decision.

Suppose the macro-prudential authority has an instrument (or vector of instruments)  $c_t$  that can be used to influence the predictive growth distribution. This influence can be direct  $(c_t \rightarrow y_{t+1})$  or indirect (e.g.,  $c_t \rightarrow s_t \rightarrow y_{t+1}$ ). The QVAR structure allows us to capture both types of transmission. A convenient way to penalize downside risk is given by specifying the utility maximization problem as

$$\max_{\{c_{t+h}\}_{h=1}^{\infty}} \sum_{h=1}^{\infty} \beta^h \Big( GL_{t,t+h} \big( y_{t+h}(c_{t:t+h}) \big) + \lambda GS_{t,t+h} \big( y_{t+h}(c_{t:t+h}) \big) \Big)$$
(15)

where  $\lambda > 1$  is a weight determining the aversion to negative realisations of output growth,  $\beta$  is an intertemporal discount factor,  $c_{t:t+h} = (c_t, \dots, c_{t+h})'$ , and  $GS_{t,t+h}$  is always a negative number.

The objective function (15) is reminiscent of the mean with downside risk model in asset allocation; see e.g. Fishburn (1977).<sup>13</sup> Since  $\mathbb{E}[y_{t+h}|\mathcal{F}_{1t}] = GS_{t,t+h}^{\tau} + GL_{t,t+h}^{\tau}$ , see Section 2.1, (15) can be rewritten in terms of expected future economic growth instead of upper quantiles to future growth. The objective function (15) is then equal to the expression suggested by Carney (2020),

$$\max_{\{c_{t+h}\}_{h=1}^{\infty}} \sum_{h=1}^{\infty} \beta^h \Big( \mathbb{E}_t \big( y_{t+h}(c_{t:t+h}) \big) + (\lambda - 1) GS_{t,t+h} \big( y_{t+h}(c_{t:t+h}) \big) \Big),$$
(16)

<sup>&</sup>lt;sup>13</sup>Kilian and Manganelli (2008) show that most of the currently existing downside risk measures are special cases of the downside risk notion proposed by Fishburn (1977) in the context of portfolio allocation.

trading off future trend growth against downside risks to the economy. We refer to Suarez (2021) for a micro-foundation of a similar objective function based on a representative agent with a CARA utility function on GDP.<sup>14</sup> We use (16) to study the benefits from adopting an active financial stability policy in Section 4.4 below.

## **3** Data

## 3.1 Macroeconomic data pre-1999

Structural QVAR models require a sufficiently large sample size to ensure that its parameters can be estimated with adequate precision. At least two challenges are present, however, when working with euro area macro data in practice. First, the euro area celebrated its 20th anniversary merely in 2019. When working with quarterly data,  $T = 4 \times 20 = 80$  is at the lower end of what is required for a meaningful empirical study of macro-financial interactions at different quantiles. Second, euro area membership has been expanding over time, from initially 11 countries in 1999 to 19 countries in 2015. Changes in euro area aggregate data stemming from new countries joining, rather than, say, from changes in financial conditions or growing vulnerabilities, would severely complicate any empirical analysis.

Fortunately, both problems can be addressed. During the ECB's early years, pre-1999 macrofinancial time series data were urgently needed for monetary policy analysis. Against this background counterfactual data were constructed "as if" the euro area had already consisted earlier; see e.g. Fagan et al. (2001). Such pre-1999 euro area data is publicly available.<sup>15</sup> We obtain real GDP growth data from 1988Q3 to 2018Q4 from this source, resulting in T = 121, and refer to Web Appendix C.1 for a time series plot.

<sup>&</sup>lt;sup>14</sup>Our empirical results presented in Sections 4.1 to 4.3 do not depend on the objective function. In Section 4.4 any other objective function could be used, if so desired, including complicated nonlinear specifications.

<sup>&</sup>lt;sup>15</sup>https://eabcn.org/page/area-wide-model. In its most recent version, the database adopts a fixed euro area composition approach, constructing aggregate data series as if the euro area had always consisted of its current (end-of-sample) 19 members. Most variables are available from 1970Q1 onwards. The further back, however, the more uncertain the data quality.

## **3.2** Composite indicator of systemic stress

The ECB's composite indicator of systemic stress (CISS) is a summary measure of the level of financial distress. Web Appendix C.1 provides a summary of the methodology, a time series plot, and a listing of all included data series. The CISS is computed for the euro area as a whole and includes 15 raw, market-based financial indicators that are split equally into five categories: financial intermediaries, money markets, equity markets, bond markets, and foreign exchange markets. Each category is summarized by a sub-index. The sub-indices are subsequently aggregated to a single time series in a way that takes their time-varying cross-correlations into account. As a result, the CISS takes higher values when stress prevails in several market segments *at the same time*, capturing the idea that financial stress is more systemic, and more dangerous for the economy as a whole, whenever financial instability spreads widely across different segments of the financial system. The CISS is updated regularly and publicly available.<sup>16</sup>

## **3.3** Real-time estimates of the financial cycle

The real-time financial cycle indicator used in the empirical analysis is based on Schüler et al. (2020). The construction of the indicator mirrors that of the CISS; see Web Appendix C.2 for details and a time series plot. Their indicator takes high values when *i*) total non-financial credit volumes grow at an unusually fast pace (proxying a credit boom), and *ii*) real estate, equity, and bond prices grow at an unusually fast pace as well *at the same time* (proxying asset price inflation). In this sense, their financial cycle indictor is not a measurement of credit growth, which can be beneficial, but of *bad*, or excess, credit growth that coincides with asset price inflation.

The financial cycle indicator is available for the euro area and the U.S. from the authors. Their indicator took high values during the dot-com boom years between 1997 and 2000, and during the credit boom years preceding the 2008–2009 global financial crisis. Their indicator took particularly low values in 2009 and 2011, times associated with crisis-induced fire sales and financial system deleveraging.

<sup>&</sup>lt;sup>16</sup>https://sdw.ecb.europa.eu/

## **4** Implementing the macro-prudential risk management approach

This section uses an estimated QVAR model to study macro-prudential policy stance in the presence of substantial asymmetries and tail interactions. It first discusses model selection, parameter estimates for a baseline specification, and the outcome of specification tests. Second, it quantifies downside risks to, and the upside potential of, the euro area economy stemming from financial stress and vulnerabilities. Third, it reports the outcome of a model stress testing exercise, assessing whether the euro area economy was at all times equally vulnerable to a fixed sequence of adverse shocks. Finally, it asks whether it pays off to adopt an active macro-prudential policy, producing a risk management-based metric of macro-prudential policy stance. We focus our discussion on the euro area, and report analogous tables and figures for U.S. data in Web Appendix F.

## 4.1 QVAR estimates

In this section, we report the estimation results of our favorite QVAR model specification. We discuss the variable selection procedure, the characteristics of the parameters estimation, specification tests, and quantile impulse response functions.

### 4.1.1 Variable selection exercise

A two-variable QVAR model for quarterly real GDP growth and the CISS provides a minimal system to study downside risks to the real economy. GDP growth is required to quantify downside risks, and the CISS significantly impacts the left tail of the predictive GDP growth distribution; see Section 4.1.2 below. This minimal system, however, may miss important interactions with other economic variables. In addition, it misses a variable that can be influenced directly through financial stability policies.

Web Appendix D discusses a systematic search over potential additional endogenous variables to be included in a QVAR. Two variables stand out as interacting closely with euro area GDP growth and financial stress at all nine quantiles. Both are related to central bank policy instruments. The de-trended three-months EURIBOR rate, a measure of monetary policy, is ranked first, impacting both future GDP growth as well as current financial conditions. Schüler et al. (2020) broad financial cycle indicator (see Section 3.3) is ranked second, followed by the euro area's capacity utilization rate. Capacity utilization is a business cycle indicator, and as such highly correlated with GDP growth, and arguably of lesser interest in a financial stability context.

Web Appendix F.2 reports analogous results for U.S. data. Approximately similar variables are selected.

### 4.1.2 Model specification and parameter estimates

We choose a trivariate QVAR specification as our benchmark model. Our benchmark model consists of annualized quarterly real GDP growth  $y_t$ , the financial cycle indicator  $c_t$ , and the CISS  $s_t$ . We therefore consider  $\tilde{x}_t = (y_t, c_t, s_t)'$ .

Figure 1 reports parameter and standard error estimates for our baseline specification. Parameter point estimates are obtained equation-by-equation via *np* univariate quantile regressions. The appropriate standard error bands around the parameter point estimates, however, do not coincide with the equation-by-equation estimates as supplied by common software packages. The standard errors reported in Figure 1 take cross-equation restrictions at common quantiles into account, see Web Appendix B.1 for details, and can be tighter or wider compared to the equation-by-equation standard error estimates.

We discuss the parameter estimates from top left to bottom right. Each of the panels presents the parameter estimates across nine deciles together with 95% confidence bands and the corresponding least squares estimate. The arrangement of panels in Figure 1 corresponds to the ordering of variables in (6). Overall, the quantile regression estimates differ substantially across quantiles, as well as from their least squares counterparts. Each intercept estimate in  $\omega$  increases monotonically in the considered quantile. This pattern is by construction, and reflects the fact that quantile shocks are not centered around zero; see (11).

## Figure 1: Parameter estimates for baseline QVAR model

Parameter estimates from a trivariate QVAR model estimated for p = 9 quantiles from 0.1 to 0.9. Variables are ordered GDP growth (respective first row), financial cycle (second row), and CISS (third row). Parameter estimates are obtained equation-by-equation while standard error estimates take cross-equation restrictions into account; see Web Appendix B.1. Standard error bands are dashed and at a 95% confidence level. Red horizontal lines indicate least squares estimates. Estimation sample is 1988Q3 to 2018Q4.



All contemporaneous effects are visible from matrix  $A_0$ . The contemporaneous impact of GDP growth on the financial cycle (element [2,1]) as well as on the CISS (element [3,1]) is small and rarely statistically significant. The [3,2]-element of  $A_0$  points to a positive contemporaneous impact of the financial cycle on the CISS at its lower quantiles. This element is a mirror image of the [3,2]-element in  $A_1$ . Taken together, they suggest that the CISS is high when the financial cycle falls (or vice versa), a pattern that also shows up in the respective impulse response function shown in Figure 2. This is intuitive, as financial sector deleveraging and financial stress tend to go hand-in-hand.

All lagged effects are visible from matrix  $A_1$ . The [1,3]-element signals the presence of substantial asymmetries in the impact that financial stress (CISS) has on future GDP growth. The [3,3]-element of  $A_1$  captures the autoregressive coefficient associated with the CISS. The estimate exceeds one at the 0.9 quantile, pointing to a local non-stationarity in the rightmost tail. Local non-stationarity is not uncommon in QAR models, and does not imply global non-stationarity; see Koenker (2005, Ch. 8.3). Indeed, conditional quantiles simulated from our QVAR model at estimated parameters converge to their unconditional counterparts. The standard errors around the locally non-stationary estimate are, however, not reliable, and not reported for this reason.

Three specifications have been run for robustness. First, the variable selection exercise in Section 4.1.1 suggested that short-term interbank rates can be a useful additional variable to consider in a QVAR. Web Appendix E.1 studies a five-variable monetary structural QVAR model. This model additionally contains the three-month EURIBOR rate as well as quarterly changes in the GDP deflator (inflation). This monetary structural QVAR model is of considerable interest in its own right. It yields, however, broadly similar predictions in terms of downside risks and measures of macro-prudential policy stance. We therefore proceed with the above more parsimonious trivariate model for simplicity.

Second, Web Appendix E.2 extends our baseline model with an additional, annual lag for all variables. Information criteria prefer the more parsimonious version. The average future growth shortfall responds more quickly, and more severely, to contemporaneous financial stress when

#### Table 1: Wald test of parameter homogeneity.

Wald tests statistics. The test's null hypothesis states that the quantile regression estimates, across p = 9 quantiles, are equal to the median regression parameter estimates. We consider our baseline trivariate QVAR model, estimated decile-by-decile, ranging from 0.1 to 0.9; see Figure 1. The test statistic is  $\chi^2$ -distributed. The appropriate degrees-of-freedom (df) are given by the number of right-hand-side variables per equation (excluding the constant, 3, 4, and 5, respectively), times the number of imposed restrictions (9 – 1 = 8).

	df	test statistic	p-value
real GDP growth, $y_t$	24	209.71	0.00
financial cycle indicator, $c_t$	32	26.12	0.76
CISS Financial stress index, $s_t$	40	79.52	0.00

based on a single-lag specification. We therefore proceed with the single-lag specification.

Finally, Web Appendix E.3 presents our baseline QVAR parameter estimates when the estimation sample is restricted to exclude counterfactual pre-1999 euro area data. The point estimates are more noisy but overall similar. The standard error bands are wider, suggesting less precise parameter estimates.

Web Appendix F.3 reports parameter and standard error estimates based on our baseline QVAR model for U.S. data. The parameter estimates are broadly in line with those for the euro area: Growing financial vulnerabilities shift the right tail of the U.S. CISS towards more positive values. A shock to the U.S. CISS shifts the left tail of the predictive GDP growth distribution towards more negative values, while leaving the right tail less affected.

#### 4.1.3 Wald test and quantile impulse response functions

Table 1 reports the outcome of three Wald  $\chi^2$  tests of parameter homogeneity across quantiles. We proceed equation by equation for i = 1, 2, 3. Each Wald test is implemented as explained in Koenker (2005, Ch. 3.3.2); see also Koenker and Basset (1982) and Web Appendix B.2. The test rejects the parameter equality restrictions implied by a linear VAR for two of our three variables, GDP growth and CISS. Parameter homogeneity is most forcefully rejected for the GDP growth equation. The test outcomes are intuitive given the parameter and standard error estimates reported

### Figure 2: Quantile impulse response functions

Impulse response functions implied by the parameter estimates reported in Figure 1. Variables are ordered as GDP growth (respective first row), financial cycle (second row), and CISS (third row). Estimation sample is 1988Q3 to 2018Q4.



in Figure 1.

Figure 2 plots quantile impulse response functions (QIRF) as implied by the parameter estimates in Figure 1. We refer to Web Appendix B.3 for a precise definition and derivation of QIRF in our modeling context. We define the QIRF as the change in the conditional quantile forecast  $q_{t+h}^{\gamma}$ , at any  $\gamma \in (0, 1)$ , when a one standard deviation (of  $\epsilon_{it}^{5}$ ) sized shock is applied to the structural shocks  $\epsilon_{it}^{\gamma}$ . In a standard VAR, there is only the mean forecast to be characterized. In a quantile VAR, one could study all the possible combinations of quantiles. In the figure, we report the impact of the shocks on different quantiles of each variable, conditioning on a median evolution of the other variables. If the data generating process were linear then the conditional median responses reported in Figure 2 would coincide with standard IRFs from a linear VAR.

The asymmetries implied by the Wald test outcomes are clearly visible in the shapes of the QIRF. As expected, the real GDP response to a shock to the CISS depends markedly on the quantile of interest. The bottom 0.1 quantile of real GDP responds much more strongly than its upper 0.9 quantile. This is not surprising, and in line with Adrian et al. (2020). The response of the CISS to a shock to the financial cycle is highly asymmetric. A shock to the financial cycle does not move the CISS much in most parts of the CISS's distribution. The upper 0.9 quantile of the CISS, however, displays a marked negative response in the short term that disappears after a year or so. Vice versa, positive shocks to the CISS depress the financial cycle approximately uniformly across the financial cycle's distribution. The interactions between the CISS and the financial cycle suggest a vicious circle to emerge during crisis periods, with an increase in financial stress triggering lower financial activity, which in turn causes stress to further increase, and so forth. Such dynamics may reflect, for example, negative externalities from financial institutions' deleveraging efforts spilling over to other segments of the financial system, with potential feedback effects, during financial turmoil.

Web Appendix F.4 discusses the analogous results for U.S. data. The Wald test outcomes and impulse response function estimates are remarkably similar across both sets of data.

## 4.2 Estimates of downside risk and upside potential

This section discusses our downside risk and upside potential estimates as introduced in Section 2.1. Web Appendix F.5 discusses the U.S. case.

Figure 3 plots the average future growth shortfall (AGS) and longrise (AGL) for the euro area. The risk estimates are based on full-sample parameter estimates, but are otherwise conditional on variables observed up to time t only. Growth shortfall and longrise are forward-looking, and averaged over t + 1 and t + 8; see (3) and (5). To study the importance of including current financial conditions and medium-term vulnerabilities we compare our baseline QVAR model to a much simpler, univariate quantile autoregressive (QAR) model for GDP growth only. The QAR model does not include the financial cycle nor the CISS.

We focus on three findings. First, accounting for financial conditions is crucial. There is a pronounced difference between the downside risk (AGS) estimate implied by the trivariate QVAR and the univariate QAR. During the global financial crisis (GFC) between 2008 and 2009, the QAR-based downside risk estimate declines much later, and by much less, compared to the QVAR-based estimate. The sovereign debt crisis between 2010 and 2012 is missed almost entirely based on the QAR model.

Second, as a result of macro-financial interactions, the QVAR's lower quantiles for future GDP growth are more volatile than its upper quantiles. This observation mirrors those of Adrian et al. (2019), who focus on single quantiles in isolation. Web Appendix E.4 plots the tail conditional expectation and expected probability of a contraction underlying  $AGS_{t,t+1:t+H}^{\tau}$  and  $AGL_{t,t+1:t+H}^{\tau}$  separately; see the first and second term in (2) and (4), respectively. Most of the variability in  $AGS_{t,t+1:t+8}^{\tau}$  comes from the changes in growth conditional on being in a recession-term, with an additional contribution from increasing the probability of a contraction in bad times.

Lastly, the downside risks implied by the QVAR model can be economically large. The GFC implied an extreme AGS over eight quarters of approximately -3.5%. This corresponds to a  $(1 - 0.035/4)^8 - 1 \approx -6.8\%$  reduction in real living standards. This is a substantial expected contraction, reflecting severe downside risks from a deterioration of financial conditions. During median times, the estimated AGS is approximately -0.5% and corresponds to a more moderate risk of a  $(1 - 0.005/4)^8 - 1 \approx -1.0\%$  reduction in real living standards.

From a risk management perspective the AGS can be compared to the AGL as the latter provides an indication of the upside for the economy. The GFC did not only generate an extremely low value for the AGS, but also for the AGL. With a value of only 0.4%, the average expected expansion of the economy over the following eight quarters would have been approximately 0.8%. This compares to an average of approximately 4% over the entire sample. The GFC thus reduced living standards especially because of the contraction, but also persistently muted the upside potential of the economy, and did so until early 2015.

#### Figure 3: Euro area AGS and AGL estimates

Time-*t* average future growth shortfall (AGS<sup> $\tau$ </sup><sub>*t*,*t*+1:*t*+8</sub>) and average future growth longrise (AGL<sup> $\tau$ </sup><sub>*t*,*t*+1:*t*+8</sub>) estimates evaluated at  $\tau = 0$ ; see (3) and (5). The trivariate estimate is based on our baseline QVAR model (dashed line, scale on left axis) that allows for macro-financial interactions. The univariate estimate is based on a one-equation restricted model with a constant and lagged GDP growth as the only right-hand-side variables (dotted line, scale on left axis). Each model is estimated for p = 20 quantiles ranging from 0.025 to 0.975. We compare these estimates to quarterly annualized real GDP growth (solid line, scale on right axis). Shaded areas indicate euro area recessions as determined by the CEPR business cycle dating committee. The estimation sample is 1988Q3 to 2018Q4.



## 4.3 Model-based stress testing

Our structural QVAR model provides a natural environment to perform model-based stress testing exercises. We here understand stress testing as a forecast of what would happen to  $\tilde{x}_t$  conditional on the system being subjected to a certain sequence of adverse shocks. We refer to such a sequence of adverse shocks as a stress scenario. For the computation of forecasts conditional on such scenarios we refer to Section 2.2.4. Our stress testing approach is different from supervisory stress tests in that our main variable of interest is not banking sector health but real economic (GDP) impact.

Figure 4 reports the time-t conditional forecast of average future real GDP growth  $\bar{y}_{t,t+1:t+4}$ between time t and t + 4 as implied by our trivariate model. The forecast is conditional on a 0.1 (conditional) quantile realization for GDP growth  $y_{t+h}$ , a 0.1 quantile realization of the financial cycle  $c_{t+h}$ , and a 0.8 quantile realization for CISS  $s_{t+h}$ , consecutively for h = 1, ..., 4. The magnitude of these shocks is approximately in line with the four observed quantile realizations for all variables between 2008Q2 and 2009Q2. The stress test is repeated at each t = 1, ..., T, and always based on the same (full sample) parameter estimates. As a result, the figure is informative about the impact of GFC-sized real and financial shocks on real living standards at any time in our sample.<sup>17</sup>

We observe that the euro area economy is not equally resilient to the same sequence of equally unlikely adverse financial shocks at all times. This is a direct consequence of the asymmetries (nonlinearities) inherent in the estimated QVAR model. When financial imbalances and financial stress are high, real GDP growth is particularly vulnerable.

Figure 4 can be informative when assessing macro-prudential policy stance. An unusually high level of vulnerability to future real and financial shocks — a value of  $\bar{\hat{y}}_{t,t+1:t+4}$  below its own 10% quantile, say — indicates that large shocks have materialized and macro-prudential buffers should be released. In the euro area, such values are observed during the financial crisis of 2008 – 2009 and the sovereign debt crisis in 2011 – 2012. Low to moderate levels of vulnerability indicate times when macro-prudential buffers could be built up. Gradually growing macro-prudential capital buffers help increase banking sector resilience, lean against bad credit growth, improve incentives, and are available to be released later whenever necessary.

Web Appendix F.6 discusses the analogous figure for U.S. data. Similar observations hold true for these data as well.

## 4.4 Towards a metric for macro-prudential policy stance

An active debate in policy circles revolves around the question of how to measure the macroprudential policy stance. In other words, should macro-prudential policy be tightened or loosened

<sup>&</sup>lt;sup>17</sup>Alternatively, one could define stress in absolute size; see e.g. Brownlees and Engle (2017) for a discussion. We prefer the quantile-based approach because the probability of the stress materializing remains constant over time regardless of current levels of volatility. The severity of stress would be much higher in periods of low volatility, as it would take a sequence of more severe shocks to reach the same level of impact. On the other hand, low volatility does not necessarily imply that the tipping point is also low.

#### Figure 4: Vulnerability to GFC-sized shocks

Dashed line: euro area annualized quarterly real GDP growth. Solid line: predicted average annualized quarterly real GDP growth  $\bar{y}_{t,t+1:t+4}$  one year ahead conditional on consecutive 0.1 quantile realizations for GDP growth  $y_t$ , 0.1 quantile realizations of the financial cycle  $c_t$ , and 0.8 quantile realizations for CISS  $s_t$ . Predictions are based on full sample parameter estimates. Estimations sample 1988Q3 – 2018Q4. Horizontal lines refer to 0.1, 0.5, and 0.9 empirical quantiles of  $\bar{y}_{t,t+1:t+4}$ .



conditional on currently-available information? We use the risk management framework of Section 2.3 and the associated objective function (16) to make a step towards addressing this question. We assume that macro-prudential instruments can be used to control the financial cycle and ask the question when it is optimal to use them.<sup>18</sup> The thought experiment of this section is the following: How does the objective function of the macro-prudential authority change if the financial cycle is marginally reduced now, to be released later on should a financial crisis occur? If the change is positive, we conclude that the macro-prudential stance is too loose (as it would benefit from a less

<sup>&</sup>lt;sup>18</sup>A complete answer to this question would require including policy instruments into our baseline model, such as bank capital and various interest rates. This can be done, at the cost of decreased model parsimony, parameter estimation precision, and identification credibility. Web Appendix E.1 suggests that our baseline downside risk and upside potential estimates are not affected, to first order, by an extension of the QVAR information set.

buoyant financial cycle). If on the other hand the answer is negative, macro-prudential policy is too tight.

Table 2 summarizes our policy experiment by contrasting two counterfactual scenarios. Each scenario looks three years into the future, equally split into two periods of H/2 = 6 quarters. The first six quarters are normal times during which the financial cycle could be marginally reduced. The second six quarters refer to a financial crisis during which the CISS takes high values and the financial cycle takes low values.

The bottom panel of Table 2 sets out an active, or marginally less passive, macro-prudential policy scenario. It is identical to the passive scenario in the top panel, except that the policy maker marginally reduces the financial cycle in the first period, for example by requiring higher counter-cyclical capital buffer requirements. During the financial crisis these buffers can be released, leading to a marginally less vicious collapse of the financial cycle. We simulate this policy by setting the financial cycle to its 0.5 quantile during  $h = 1, \ldots, 6$ , instead of 0.6, and to its 0.2 conditional quantile during  $h = 7, \ldots, 12$ , instead of 0.1. The evolution of GDP growth is always unrestricted. Doing so allows us to simulate forward the GDP growth rate,  $y_{t+h}$ , and growth shortfall,  $GS_{t,t+h}$ , at any time t + h,  $h = 1, \ldots, 12$ .

Each policy scenario is evaluated as

$$u_t \left( \text{Scenario} \right) = \hat{\bar{y}}_{t+1:t+12} \left( \text{Scenario} \right) + 0.50 \cdot \hat{A} \hat{GS}_{t,t+1:t+12} \left( \text{Scenario} \right), \tag{17}$$

where the mean growth estimate  $\hat{y}_{t+1:t+12}$  and average future growth shortfall estimate  $\hat{A}G\tilde{S}_{t,t+1:t+12}$ are obtained from 10,000 simulations of potential future  $y_{t+h}$ . The utility function (17) operationalizes (16) by choosing parameters as  $\beta = 1$  for h = 1, ..., 12 and  $\beta = 0$  thereafter,  $\lambda = 1.50$ , and  $\tau = 0$ . Our choice of the penalty term  $\lambda$  implies that the policy maker cares twice as much (positively) about future trend growth than she cares (negatively) about downside risk. We evaluate (17) twice, once for the active scenario and once for the passive scenario, and study the difference between the two at any time t.

#### Table 2: Passive vs. active macroprudential policy

The top and bottom panels report selected quantiles for GDP growth  $(y_t)$ , financial cycle  $(c_t)$ , and CISS  $(s_t)$  under a passive and active macroprudential policy benchmark, respectively. Multiple quantiles 0.1 - 0.9 mean that the quantile is picked at random. The first six quarters are normal times during which the financial cycle could, in principle, be marginally reduced. The second six quarters refer to a financial crisis during which the CISS takes high values and the financial cycle takes low values. If the financial cycle is actively managed in the first period then it does not not have to contract as much during the crisis.

		first six quarters	second six quarters
		"normal times"	"financial crisis"
passive	$y_t$	0.1 – 0.9	0.1 – 0.9
benchmark	$c_t$	0.6	0.1
	$s_t$	0.1 - 0.9	0.9
active	$y_t$	0.1 – 0.9	0.1 - 0.9
macro-pru	$c_t$	0.5	0.2
policy	$s_t$	0.1 – 0.9	0.9

Figure 5 plots the utility difference  $\Delta u_t = u_t$  (active)  $-u_t$  (passive) associated with adopting the active macro-prudential policy. Adopting the active policy is the preferred option most of the time. This is not surprising as we condition on a severe financial crisis in the second period. Adopting the active policy, however, is not equally beneficial at all times. The benefits from leaning against the financial cycle are maximal during the late 1990s before the bust of the dot-com boom in 2000, and during the mid-2000s before the onset of the global financial crisis in 2007. This is intuitive, as the financial system was buoyant during these times, arguably seeding the respective busts later on. The benefits from leaning against the financial cycle are estimated to be the most negative following the global financial crisis of 2008, and during the euro area sovereign debt crisis between 2010 and 2012. This is again intuitive, as the financial system was already deleveraging during these times, and requiring more would add insult to injury. The utility difference  $\Delta u_t$  is mildly correlated with the euro area financial cycle, suggesting that it is a valuable variable to track to inform macroprudential policy discussions.

Web Appendix F.7 derives a stance metric for U.S. data. Adopting an active financial stability policy remains the preferred policy when the financial cycle is buoyant.

#### Figure 5: The benefits from active macro-prudential policy

The benefit of adopting an active macro-prudential policy stance in utility terms,  $\Delta u_t = u_t$  (active) –  $u_t$  (passive); see (17). Parameters are chosen as  $\beta = 1$ ,  $\lambda = 1.5$ ,  $\tau = 0$ , and H = 12. The difference is based on full sample estimates. Estimation sample is 1988Q3 to 2018Q4. Shaded areas indicate euro area recessions.



## 5 Conclusion

We proposed a risk management approach to macro-prudential policy that relates downside risks and upside potential of the economy to measures of financial stress and medium-term vulnerabilities. In an empirical study of euro area and U.S. data we found evidence of substantial asymmetries in the conditional distribution of GDP. The left quantiles of the predictive GDP growth distribution are related to a contemporaneous indicator of systemic stress, whose right quantiles are related to financial vulnerabilities. Counterfactual exercises allow us to perform model based stress testing, to construct urgently-needed indicators of macro-prudential policy stance, and to assess when macro-prudential interventions are relatively more likely to be beneficial.
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# A The non-cyclicality of the counter-cyclical capital buffer

Figure A.1 plots the evolution of required counter-cyclical capital buffers (CCyB) for banks located in 28 European Union countries (top panel) and 19 euro area countries (bottom panel) between 2014 and 2019. By December 2019, five years after the introduction of CCyB, less than one in three countries have moved to positive CCyBs. The majority of countries have not activated this financial stability tool, in line with a potential inactivity bias.

#### Figure A.1: The non-cyclicality of the counter-cyclical capital buffer

Required counter-cyclical capital buffers for banks located in 28 European Union countries (top panel) and 19 euro area countries (bottom panel) between 2014 and 2019. Country abbreviations are as in *www.esrb.europa.eu/nationalpolicy/ccb/html/index.en.html*. The size of the circles is proportional to the number of countries for which the CCyB takes a certain value. Source: end-of-year data from the European Systemic Risk Board.



# **B.1** Parameter estimation and standard errors

The recursive QVAR model (10) – (11) can be estimated using the framework developed by White et al. (2015). Let  $q_t^{\gamma}(\beta) \equiv \omega^{\gamma} + A_0^{\gamma}Y_t + A_1^{\gamma}Y_{t-1}$  and  $q_{it}^{\gamma_j}(\beta)$  the  $j^{th}$  quantile of the  $i^{th}$  variable of the vector  $q_t^{\gamma}(\beta)$ , where we have made explicit the dependence on  $\beta$ , the vector containing all the unknown parameters in  $\omega^{\gamma}$ ,  $A_0^{\gamma}$ , and  $A_1^{\gamma}$ . Define the quasi-maximum likelihood estimator  $\hat{\beta}$  as the solution of the optimization problem

$$\hat{\beta} = \arg\min_{\beta} T^{-1} \sum_{t=1}^{T} \left\{ \sum_{i=1}^{n} \sum_{j=1}^{p} \rho_{\gamma} \left( \tilde{Y}_{it} - q_{it}^{\gamma_j}(\beta) \right) \right\},\tag{B.1}$$

where  $\rho_{\gamma}(u) \equiv u(\gamma - I(u < 0))$  is the standard check function of quantile regressions; see also Koenker and Bassett (1978) and Engle and Manganelli (2004). The asymptotic distribution of the regression quantile estimator is provided by White et al. (2015), which we report here for convenience.

Under the assumptions of Theorems 1 and 2 of White et al. (2015),  $\hat{\beta}$  is consistent and asymptotically normally distributed. The asymptotic distribution is

$$\sqrt{T}(\hat{\beta} - \beta^*) \xrightarrow{d} N(0, Q^{-1}VQ^{-1}), \tag{B.2}$$

where

$$Q \equiv \sum_{i=1}^{n} \sum_{j=1}^{p} E[f_{it}^{\gamma_j}(0) \nabla q_{it}^{\gamma_j}(\beta^*) \nabla' q_{it}^{\gamma_j}(\beta^*)]$$
$$V \equiv E[\eta_t \eta_t']$$
$$\eta_t \equiv \sum_{i=1}^{n} \sum_{j=1}^{p} \nabla q_{it}^{\gamma_j}(\beta^*) \psi^{\gamma_j}(\epsilon_{it}^{\gamma_j})$$
$$\psi^{\gamma_j}(\epsilon_{it}^{\gamma_j}) \equiv \gamma_j - I(\epsilon_{it}^{\gamma_j} \le 0)$$
$$\epsilon_{it}^{\gamma_j} \equiv \tilde{Y}_{it} - q_{it}^{\gamma_j}(\beta^*)$$

and  $f_{it}^{\gamma_j}(0)$  is the conditional density function of  $\epsilon_{it}^{\gamma_j}$  evaluated at 0.

The asymptotic covariance matrix can be consistently estimated as suggested in Theorems 3 and 4 of White et al. (2015), or using bootstrap-based methods following Buchinsky (1995). Modern statistical softwares typically contain packages for quantile regression estimation and inference that estimate the above quantities. Our paper uses the interior point algorithm discussed by Koenker and Park (1996) and as implemented in Stata.

# **B.2** Wald test for slope parameter homogeneity

The classical theory of linear regression *assumes* that the conditional quantile functions of the response variable given covariates are all parallel to one another. In our model, linearity implies that the slope parameters  $A_{0,i}^{\gamma}$ ,  $A_{1,i}^{\gamma}$  (i.e. parameters other than the constant  $\omega_i$ ), i = 1, ..., n, associated with different  $\gamma$ s are identical across  $\gamma$ s. Changes in covariates then shift the location of the response distribution but do not change its scale or shape. In many applications, however, quantile regression parameter estimates often vary considerably across quantiles. As a result, an immediate and fundamental problem of inference in QR models involves testing for equality of slope parameters across quantiles. We proceed equation by equation for i = 1, 2, 3, reporting a test statistic for each equation. The Wald test is implemented as explained in Koenker and Basset (1982); see also Koenker (2005, Ch. 3.3.2).

### **B.3** Impulse response functions

This section derives impulse response functions (IRF) for our structural QVAR model. If the recursive model can be given a structural interpretation, it is possible to derive a structural quantile impulse response function. We first express  $x_t$  in terms of structural shocks,

$$x_t = \nu + Bx_{t-1} + (I_{np} - A_0)^{-1} \epsilon_t,$$

where  $\nu = (I_{np} - A_0)^{-1}\omega$  and  $B = (I_{np} - A_0)^{-1}A_1$ . In a standard VAR model, a shock to variable *i* at *t* is affecting only the conditional expectations. In the case of QVAR, the same shock is affecting all the quantiles. We define the shock to the structural residuals of variable *i*, for i = 1, ..., n, as

$$\ddot{\epsilon}^i_t = \epsilon_t + s^i \delta_t$$

where  $\delta \in \mathbb{R}$  and  $s^i$  is an np vector of zeros with p ones in the positions corresponding to the quantile residuals of the  $i^{th}$  variable. A straightforward choice for  $\delta$  is one standard deviation of the estimated median shocks  $\epsilon_{it}^5$ . The shock  $\delta$  is simultaneously applied to all the quantile structural shocks of the  $i^{th}$  variable. Denoting with  $\ddot{x}_t$  the value of the dependent variables if the shock  $\ddot{\epsilon}_t^i$  is applied, the impulse response function at time t + h can then be defined recursively as

$$\Delta_t^i \equiv \ddot{x}_t - x_t$$
  
=  $(I_{np} - A_0)^{-1} s^i \delta$  (B.3)

$$\Delta_{t+1}^i = C_{t+1} A_1 \Delta_t^i \tag{B.4}$$

$$\Delta_{t+h}^{i} = C_{t+h} A_1 \bar{S} \Delta_{t+h-1}^{i} \qquad \text{for } h \ge 2, \tag{B.5}$$

where  $C_{t+h} \equiv (I_n - S_{t+h}^{\gamma^h} A_0 \bar{S})^{-1} S_{t+h}^{\gamma^h}$  and  $\bar{S}$  have been defined in Section 2.2.4. While the *C* matrix can be defined to identify any possible sequence of quantiles, the example reported in Figure 2 of the paper refers to the case where the QIRFs of the variable under study are conditional on the

forecast of the other two variables being equal to their median.

Notice that if one were to model only the median, this would coincide with the median impulse response analogue of the standard mean impulse response function. Quantile impulse response functions, however, will generally depend on the quantiles paths which are considered.

## **B.4** Simulation algorithm for downside risk measures

Let t = 1, ..., T denote any time in our sample. We obtain time-t conditional downside risk measures by simulating forward S = 10,000 potential future paths for all n variables in  $\tilde{x}_{i,t+h}$ , h = 1, ..., 8 quarters ahead.

We proceed as follows.

- Fix any t = 1,...,T. Obtain and save full-sample parameter estimates for all variables at all p = 20 quantiles 0 < 0.025, 0.075, ..., 0.925, 0.975 < 1. Set s = h = 1.</li>
- Draw n standard uniform random variables u<sub>i,t+h</sub>, one for each variable 1,...,n. Select variable-specific quantiles γ<sub>i,t+h</sub> that are closest to u<sub>i,t+h</sub>, respectively. Combine the chosen rows ω<sub>i</sub><sup>γ<sub>i,t+h</sub>, A<sub>0,i</sub><sup>γ<sub>i,t+h</sub></sup>, A<sub>1,i</sub><sup>γ<sub>i,t+h</sub></sup> into QVAR parameter matrices ω<sup>γ</sup>, A<sub>0</sub><sup>γ</sup>, A<sub>1</sub><sup>γ</sup>.
  </sup>
- 3. Predict  $x_{t+h}$  one-step ahead using (6); see also (B.7).
- 4. Compute and save downside risk estimates  $GS_{t,t+h}^{\tau}$  and  $GL_{t,t+h}^{\tau}$  by evaluating the sample analogues of (2) and (4). For example,

$$\mathbf{GS}_{t,t+h}^{\tau,(s)} = \tilde{x}_{1,t+h}^{(s)} \cdot 1\{\tilde{x}_{1,t+h}^{(s)} < \tau\},\$$

where  $\tilde{x}_{1,t+h}^{(s)}$  denotes a simulated value for quarterly real GDP growth at time t + h.

5. If h < H, set h = h + 1 and return to step 2. If h = H, compute  $AGS_{t,t+1:t+h}^{\tau}$  and  $AGL_{t,t+1:t+h}^{\tau}$  by averaging over  $GS_{t,t+h}^{\tau}$  and  $GL_{t,t+h}^{\tau}$ . Save these simulation-specific risk estimates.

6. If s < S, increase s = s + 1 and return to step 2. If s = S, compute final time-t downside risk measures as averages across simulation runs.

### **B.5** Counterfactual scenarios

Rather than moving through the complete tree of potential future values of  $\tilde{x}_{t+h}$  at random, as explained in Web Appendix B.4, we may at other times wish to consider only one path in isolation. Such a path in isolation can also be thought of as a 'counterfactual scenario,' or model-based thought experiment that conditions on an arbitrary but fixed sequence of future shocks.

The quantile of each element of the vector  $x_{t+1}$  at time t is a random variable, as, except for the first element, it depends on the contemporaneous shocks of the other variables. Given the recursive identification assumption, we can forecast the quantiles conditional on any desired quantile shock realization. To this end we define a sequence of selection matrices  $\{S_{t+h}^{\gamma^h}\}_{h=1}^H$ , with typical  $[n \times np]$  element  $S_{t+h}^{\gamma^h}$  selecting specific quantile shocks from the  $[np \times 1]$  vector  $\epsilon_{t+h}$  (see (10)), one shock for each variable i:

$$S_{t+h}^{\gamma_{h}^{h}}\epsilon_{t+h} \equiv [\epsilon_{1,t+h}^{\gamma_{t+h}^{1}}, \dots, \epsilon_{n,t+h}^{\gamma_{t+h}^{n}}]', \tag{B.6}$$

for  $\gamma_{t+h}^i \in {\gamma_1, \ldots, \gamma_p}$  and  $i \in {1, \ldots, n}$ , selecting the variable-specific shocks to be set to zero.<sup>1</sup> By (6)–(7), the quantile forecast of  $\tilde{x}_{t+1}$ , conditional on setting the quantile shocks identified by the matrix  $S_{t+h}^{\gamma^h}$  to zero, is

$$\hat{x}_{t+1}^{S} = C_{t+1}(\omega + A_1 \tilde{x}_t)$$
(B.7)

$$\hat{x}_{t+h}^{S} = C_{t+h}(\omega + A_1 \bar{S} \hat{x}_{t+h-1}^{S}) \quad \text{for } h \ge 2$$
 (B.8)

where  $C_{t+h} \equiv (I_n - S_{t+h}^{\gamma^h} A_0 \bar{S})^{-1} S_{t+h}^{\gamma^h}$ , and where  $\bar{S}$  is a  $[np \times n]$  matrix such that  $x_{t+h} = \bar{S} S_{t+h}^{\gamma^h} x_{t+h}$ .<sup>2</sup>

Given the above sequence  $\{S_{t+h}^{\gamma^h}\}_{h=1}^H$ , it is now possible to iterate the system (B.7)-(B.8) for-

<sup>&</sup>lt;sup>1</sup>Recall that zero is not a neutral value except for the median; see (11).

 $<sup>{}^{2}\</sup>bar{S}$  consists of stacked identity matrices and is always available and unique. The selection of variable-specific quantiles via (B.6) does not lead to a loss of information.

ward to obtain forecasts of the dependent variables  $\tilde{x}_{t+h}$  at any future point h conditional on the specified counterfactual scenario.

# C Data details

## C.1 CISS: construction details and data sources

The Composite Indicator of Systemic Stress (CISS) belongs to the family of financial stress indices (FSIs). FSIs are generally designed to quantify the level of stress in the whole or parts of the financial system. They do this by aggregating a certain number of individual stress indicators into a single statistic; see Illing and Liu (2006) and Kliesen et al. (2012) for surveys. The individual components capture market- and instrument-specific stress symptoms, such as increased market volatility, default risk premia, or liquidity risk premia.

The distinctive feature of the CISS is its focus on the *systemic* dimension of financial stress. Systemic stress is interpreted as an *ex post* measure of systemic risk, i.e. a measure of the degree to which systemic risk materialised. It builds on standard definitions of systemic risk characterising it as the risk that financial instability becomes so widespread that it severely disrupts the provision of financial services to the broader economy with significant adverse effects on growth and employment; see e.g. de Bandt and Hartmann (2000) and Freixas et al. (2015, p. 13). The CISS operationalises the idea of systemic stress by aggregating market-specific subindexes of stress based on time-varying correlations between them in the same way portfolio risk (variance) is computed from the risk profiles of individual assets (variances and covariances). In this way the CISS puts more weight on situations in which stress prevails in several market segments at the same time. This is consistent with the idea that stress becomes systemic when it is correlated and widespread. Table C.1 provides a description of all CISS components.

The CISS is computed as follows. First, 15 stress indicators are selected from five major segments of the financial system. The five market segments are i) the financial intermediaries sector, ii) money markets, iii) bond markets, iv) equity markets for non-financial firms, and v) foreign exchange markets. Taken together, these segments cover the main financial flows from lenders to ultimate borrowers. The financial funds are allocated either directly via securities markets, or indirectly through financial intermediaries.

#### Table C.1: Components of the CISS

A listing of variables and transformations used in the computation of the CISS. Volatility is computed as a weekly average of absolute daily log return or interest rate changes. CMAX computed based on end-of-week values. All other series are computed as weekly averages of daily data. Data start in January 1980 or when becoming available. Data sources are Thomson Financial Datastream, ECB, and own calculations. Weekly updates of the CISS are available from the ECB's Statistical Data Warehouse (SDW). The SDW key is CISS.D.U2.Z0Z.4F.EC.SS\_CI.IDX.<sup>3</sup>

	Sector and variables	weight
A.	Money markets	0.15
A.1	Volatility of 3-month Euribor.	
A.2	Spread between 3-month Euribor and French Treasury bill rate.	
A.3	Monetary Financial Institutions' recourse to the ECB's marginal lending facility	
	divided by total reserve requirements.	
В	Bond markets	0.15
<b>B</b> .1	Volatility of German 10-year benchmark government bond prices.	
B.2	7-year yield spread between A-rated non-financial corporate and government bonds.	
B.3	10-year interest rate swap spread.	
C.	Equity markets	0.25
C.1	Volatility of non-financial stock price index.	
C.2	Maximum cumulated loss (CMAX) of non-financial stock price index	
	over a moving 2-year window; $CMAX_t = 1 - x_t / \max[x_i \in (x_{t-j}   j = 0, 1,, 104)].$	
C.3	Stock-bond return correlation between total market stock price index and German	
	10-year government bonds. Computed as difference between moving 4-week and 4-year	
	windows to account for trend changes. Negative differences are set to zero.	
D.	Financial intermediaries	0.30
D.1	Volatility of financial stock price index.	
D.2	Geometric average of the CDF-transformed CMAX and the book-price ratio	
	associated with a financial stock price index.	
D.3	7-year yield spread between A-rated financial and non-financial corporate bonds.	
E.	Foreign exchange markets	0.15
E.1	Volatility of euro exchange rate vis-à-vis US dollar.	
E.2	Volatility of euro exchange rate vis-à-vis Japanese Yen.	
E.3	Volatility of euro exchange rate vis-à-vis British pound.	

Second, all indicators are transformed by applying a probability integral transform (PIT) based on their empirical cumulative distribution function. For this purpose, the T observations of an indicator  $x_t = (x_1, x_2, ..., x_T)$  are first ranked in ascending order, i.e.  $x_{[1]} \le x_{[2]} \le ... \le x_{[T]}$ , where  $x_{[1]}$  represents the sample minimum and  $x_{[T]}$  the maximum. The transformed indicators  $z_t$  result from replacing each original observation  $x_t$  with its respective empirical cumulative distribution function value  $F(x_t)$ . That value can be computed as the ranking number r of observations not exceeding a particular value  $x_t$ , divided by the total number of available observations T.

$$z_t = F(x_t) := \begin{cases} \frac{r}{T} \text{ for } x_{[r]} \le x_t < x_{[r+1]}, r = 1, 2, ..., T - 1\\ 1 \text{ for } x_t \ge x_T. \end{cases}$$
(C.1)

The transformation results in indicators which are unit-free and unconditionally uniformly distributed over the unit interval. The transformed indicators are thus homogenous in terms of scale and distribution. The PIT also robustifies the composite indicator to outliers. This is an important property since the CISS is computed recursively over an expanding data window. The construction of the CISS avoids look-ahead bias and event reclassification problems; see e.g. Hollo et al. (2012) and Brownlees et al. (2020). For each market segment i = 1, 2, ..., 5, we compute a stress subindex  $s_{it}$  from j = 1, 2, 3 transformed components  $z_{ijt}$  as a simple arithmetic average:  $s_{it} = \frac{1}{3} \sum_{j=1}^{3} z_{ijt}$ .

Finally, the last aggregation step requires an estimate of time-varying cross-correlations between the  $s_{it}$ . We estimate the variance-covariance matrix  $H_t$  of the 5-dimensional vector of demeaned subindexes  $\tilde{s}_t = (s_t - 0.5)$  as an exponentially-weighted moving average (EWMA), according to which

$$H_t = \lambda H_{t-1} + (1-\lambda)\widetilde{s}_t \widetilde{s}'_t, \tag{C.2}$$

with a smoothing parameter fixed at  $\lambda = 0.93$ . This is a common choice for daily or weekly data; see Engle (2002). The elements  $\omega_{ijt}$  of correlation matrix  $\Omega_t$  are computed from the elements  $h_{ijt}$ 

#### Figure C.1: Euro area real GDP growth rate, CISS, and financial cycle indicator

Left panel: The GDP growth rate is annualized (left scale). The CISS varies between 0 and 1 by construction (right scale). Right panel: The real-time broad financial cycle indicator of Schüler et al. (2020). The financial cycle indicator takes high values when total non-financial credit volumes grow at a fast pace, and real estate, equity, and bond prices grow at a fast pace as well. Shaded areas indicate CEPR euro area recession periods.



of  $H_t$  as  $\omega_{ijt} = h_{ijt} / \sqrt{h_{iit} h_{jjt}}$ . The CISS is now computed as

$$CISS_t = (w \cdot z_t)'\Omega_t(w \cdot z_t), \tag{C.3}$$

where  $0 < CISS_t \le 1$  by construction. The vector of market segment weights w is given in the last column of Table C.1 and is chosen to be approximately in line with euro area national accounts and preliminary data analysis; see Hollo et al. (2012) for details.

The left panel of Figure C.1 reports euro area GDP growth along with the CISS between 1988Q3 and 2018Q4. High values of the CISS are observed during the recession in 1992, the global financial crisis between 2008 and 2009, and during the euro area sovereign debt crisis between 2010 and 2012. In each case, elevated financial stress is associated with negative GDP growth.

# C.2 Financial cycle indicator details

This subsection sketches the construction of Schüler et al. (2020)'s broad financial cycle indicator for convenience. The main purpose of the indicator is to capture a build-up of financial imbalances.

The indicator is constructed as follows. First, quarterly growth rates of total credit volume, real estate prices, equity prices, and bond prices are obtained. Second, the four series are combined using the CISS methodology as detailed in Section C.1. This approach ensures that the indicator emphasizes times when all four sub-indicators take high values simultaneously. Third, the resulting time series is smoothed by taking a weighted average over a rolling window covering the last six quarters. The weights decline linearly  $(6/21, 5/21, \ldots, 1/21)$ , with the highest weight on the most recent observation. The latter step serves to trade off reliability (fewer erratic movements) against timeliness (ability to react to recent developments in a timely fashion). The indicator is shown to have out-of-sample early warning properties viz-à-viz financially led downturns.

# **D** Euro area variable selection exercise

This section presents the main results of a systematic search over potential additional endogenous variables to be included in a QVAR.

Our variable selection exercise is set up as follows. We estimate a recursive trivariate QVAR for  $\tilde{x}_t = (y_t, z_t, s_t)'$ , consisting of annualized quarterly real GDP growth  $y_t$ , a third variable  $z_t$  to be affected by macroprudential policies, and the CISS  $s_t$ . Sandwiching  $z_t$  between  $y_t$  and  $s_t$  implies that  $z_t$  can explain  $s_t$  (the CISS) both instantaneously and with a lag. We loop over many available macro-financial variables  $z_t$ . For each case we evaluate the average quantile regression objective function at quantiles ranging from 0.1 to 0.9 (decile-by-decile). The objective function is evaluated only for the GDP growth and CISS equations, as these variables remain fixed across loops. Each trivariate system is estimated for the same number of data points and deterministic model parameters. As a result, information criteria penalty terms are the same across specifications, and can therefore be set to zero for model comparison purposes without loss of generality.<sup>4</sup>

Figure D.1 presents our main variable selection results for the euro area. Variables are ranked in terms of average check function values – the smaller the better. Non-stationary time series are de-trended using Hamilton (2018)'s filter, and are marked with a star (\*) in the figure legend.

Two variables stand out as interacting closely with euro area GDP growth and financial stress at all nine quantiles. Both are related to central bank policy instruments. The de-trended threemonths EURIBOR rate, a measure of monetary policy, is ranked first, impacting both future GDP growth as well as current financial conditions. Schüler et al. (2020) broad financial cycle indicator (see Section 3.3) is ranked second, followed by the euro area's capacity utilization rate. Capacity utilization is a business cycle indicator, and as such highly correlated with GDP growth, and arguably of lesser interest in a financial stability context.

Table D.1 lists all macro-financial variables used in our variable selection exercise; see Section 4.1.1. The list for variable selection is close to that advocated by Aikman et al. (2017). Non-stationary time series were detrended using Hamilton (2018)'s regression filter.

<sup>&</sup>lt;sup>4</sup>For a discussion of model selection between different quantile time series models see e.g. Lee et al. (2014).

#### Figure D.1: Variable selection

Variables are ranked according to their average check function value in a three-variable QVAR. Real quarterly GDP growth and CISS are fixed variables in the QVAR. Check function variables are evaluated at quantiles from 0.1 to 0.9 (decile-by-decile) for US GDP growth and US CISS only. Estimation sample is 1976Q2 to 2018Q4. Non-stationary time series are de-trended using Hamilton (2018)'s regression filter and are indicated in the legend with a asterisk (\*).



- 1 3-Month Euribor
- 3 Capacity Utilization Rate\*
- 5 Systemic Risk Indicator (Mean), EA19\*
- 7 EURO STOXX 50 Price Index
- 9 House Price Index-DPI Ratio, EA17
- 11 House Price Index, EA17
- 13 House Price Index
- 15 Standardised House Price Index-DPI Ratio
- 17 Current Account Balance as a Share of GDP\*
- 19 House Price Index-Rent Price Index Ratio, EA17
- 21 Unemployment Rate\*
- 23 Total Employment

- 2 Broad FinCycle Indicator\*
- 4 Loans to Households (HHs) and Non-Profit Orgs Serving HHs
- 6 Systemic Risk Indicator (Median), EA19\*
- 8 News-Based Economic Policy Uncertainty Index\*
- 10 Standardised House Price Index-DPI Ratio, EA17
- 12 10-Year US-Euro Area Interest Rate Spread
- 14 Narrow FinCycle Indicator
- 16 House Price Index-DPI Ratio
- 18 Standardised House Price Index-Rent Price Index Ratio, EA17
- 20 Loans to Non-Financial Corporations
- 22 10-Year Government Bond Yield
- 24 Gross Household Saving Rate

## Table D.1: Variables list for the selection exercise

Euro area variables used in the selection exercise discussed in Section 4.1.1.

Variable	Description	Source
Total employment	Euro area total employment,	Euro area wide model
	calendar and seasonally adjusted, in thousands	
Unemployment rate	Euro area unemployment rate,	Euro area wide model
	share of civilian workforce, S.A. (%)	
HH savings rate	Euro area gross household saving rate,	Euro area wide mode
C	calendar and seasonally adjusted.	
10-year Government bond yield	Euro area nominal long-term interest rate	Euro area wide model
	In percent, and per annum	
3-Month Euribor	Euro area nominal short-term interest rate,	Euro area wide model
	Last trade price, percent per annum	
Loans to HHs	Euro area loans to households,	Euro area wide model
	at current prices, market value, in Euro (Billions)	
Loans to non-financial corporations	Euro area loans to non-financial corporations,	CEPREMAP
Loans to non-inflancial corporations	at current prices and market values, in euro (Billions)	CEF KEWIAF
Consolity utilization note	EA total manufacturing capacity utilization rate	Datastream
Capacity utilization rate		Datastream
TT · · 1	seasonally adjusted, monthly average over EA19 (%)	OFOD
House price index	Euro area residential property price index,	OECD
	real value (2015=100)	
House price index - DPI ratio	Euro area residential property price index	OECD
	to per capita net nominal disposable income, ratio (%)	
House price index, EA17	Euro area residential property price index,	OECD
	real value (2015=100). EA17	
House price to rent ratio	Euro area residential property price index	OECD
	to rent price index ratio. EA17 (%)	
Systemic risk indicator (Median)	Median of the systemic risk indicator,	ECB
	taken over EA19	
Systemic risk indicator (Mean)	Mean of systemic risk indicator,	ECB
	taken over EA19	
Broad financial cycle indicator	Broad financial cycle indicator	Schüler, Hiebert,
	·	and Peltonen (2020)
Narrow financial cycle indicator	Narrow financial cycle Indicator	Schüler, Hiebert,
·	·	and Peltonen (2020)
10-year US-EA interest rate spread	10-year US-EA interest rate,	ECB
ji	spread, end of period, percent per annum	
EURO STOXX 50 index	EURO STOXX 50 price index	ECB
	monthly average	LOD
Current account balance	EA current account balance	ECB
	as a share of GDP. EA19 (%)	
Policy uncertainty index	News-based economic policy uncertainty index,	
i oney uncertainty index	News index (mean=100)	
	news muex (mean=100)	

# E Additional results for euro area data

## E.1 Robustness to extending the QVAR information set to five variables

This section considers an alternative five-variable QVAR model specification. The extended model contains quarterly changes in the GDP deflator (inflation) and the three-month EURIBOR interest rate as additional endogenous variables to the reference specification described in Section 4.1.2. The monetary policy rate is ordered last, as the central bank sets it in a systematic, forward-looking way (that is, however, not modeled further). The quarterly changes in the GDP deflator are ordered first, and thus does not react contemporaneously to the other four variables. The ordering of variables in the estimated QVAR is thus: GDP inflation, real GDP growth, financial cycle, CISS, monetary policy interest rate.

Figure E.1 plots downside risk (average future growth shortfall) based on the extended fivevariable model. Our baseline AGS sstimates are provided as a point of comparison; see Figure 3. Both model specifications yield broadly similar predictions in terms of downside risk. We therefore proceed with the more parsimonious trivariate model for simplicity.

## E.2 Robustness to changes in lag length

This section considers an alternative model specification with an extended lag structure. The alternative model retains the baseline three variables as endogenous variables, but allows for a lag at the fourth quarter in addition to the first lag (q = 1, 4). Figure E.2 is analogous to Figure 3. Information criteria prefer the more parsimonious version. Average future growth shortfall responds more quickly, and more severely, to contemporaneous financial stress when based on a single-lag specification.

## E.3 Parameter estimates from a restricted sample

Figure 1 reports our baseline QVAR parameter estimates when the estimation sample is restricted to exclude counterfactual pre-1999 euro area data. The point estimates are more noisy but overall

similar. The standard error bands are wider, suggesting less precise parameter estimates.

# E.4 Tail conditional expectation and contraction probability

Time-*t* average future growth shortfall  $AGS_{t,t+1:t+8}^{\tau}$ , and average future growth longrise  $AGL_{t,t+1:t+8}^{\tau}$  consist of two factors: a tail conditional expectation term, and the probability of a contraction; see (2) and (4). The top and bottom panel of Figure E.4 plot the first and second factor over time, respectively. Most of the variability in  $AGS_{t,t+1:t+8}^{\tau}$  comes from the first term, with an additional contribution of the second term in bad times.

#### Figure E.1: Average future growth shortfall estimates for euro area data

Growth shortfall estimates based on a five-variable QVAR including, in addition, quarterly changes in the log GDP deflator (i.e., inflation) and the three-month EURIBOR interest rate as additional endogenous variables. Our baseline growth shortfall estimates are provided as a point of comparison; see Figure 3. Shaded areas indicate CEPR recessions. The estimation sample is 1988Q3 to 2018Q4.



#### Figure E.2: Average future growth shortfall estimates for euro area data

Growth shortfall estimates based on a three-variable QVAR with an extended lag structure (q = 1, 4). Our baseline growth shortfall estimates are provided as a point of comparison; see Figure 3. Shaded areas indicate CEPR recessions. The estimation sample is 1988Q3 to 2018Q4.



### Figure E.3: Parameter estimates for 1999Q1 – 2018Q4 restricted sample

Parameter estimates from a trivariate QVAR model estimated for p = 9 quantiles from 0.1 to 0.9. Estimation sample is 1999Q1 to 2018Q4. Variables are ordered GDP growth (respective first row), financial cycle (second row), and CISS (third row). Parameter estimates are obtained equation-by-equation while standard error estimates take cross-equation restrictions into account; see Web Appendix B.1. Standard error bands are dashed and at a 95% confidence level. Red horizontal lines indicate least squares estimates.



#### Figure E.4: Euro area AGS and AGL components

Top panel: average future conditional tail expectation; see first factor in (2) and (4). Bottom panel: average future contraction probability; see second factor in (2) and (4). Each estimate is based on p = 20 quantiles ranging from 0.025 to 0.975. The threshold  $\tau$  is set to zero; see Figure 3. We compare these estimates to quarterly annualized real GDP growth (solid line, left scale). Shaded areas indicate euro area recessions as determined by the CEPR business cycle dating committee. The estimation sample is 1988Q3 to 2018Q4.



# F Selected results for U.S. data

# F.1 U.S. data

The left panel of Figure F.1 reports U.S. quarterly annualized real GDP growth along with the CISS between 1973Q1 and 2018Q4. Shaded areas indicate recession periods according to the NBER business cycle dating committee. Similar to the euro area regularities, high values of the CISS for the U.S. are clearly associated with negative realizations of real GDP growth.

The right panel of Figure F.1 plots Schüler et al. (2020)'s broad financial cycle indicator for the U.S. Their indicator took high values in the years leading up to the U.S. savings and loan crisis during 1982 and 1984, during the dot-com boom years between 1997 and 2000, and during the "conundrum" period between 2003 and 2006 preceding the financial crisis.

#### Figure F.1: U.S. real GDP growth rate, CISS, and financial cycle indicator

The GDP growth rate is annualized. Shaded areas indicate NBER recession periods. CISS and FCY vary between 0 and 1 by construction.



# F.2 Variable selection results for U.S. data

This section reports the results from a variable selection exercise for U.S. data. The setup of the exercise is analogous to the one presented in Section 4.1.1. We study which variable is most appropriate to be added to a baseline bivariate QVAR containing real GDP growth and U.S. CISS based on the average QR "check" objective function; see Koenker and Bassett (1978).

Figure F.2 presents our variable selection results. Remarkably, the highly-ranked variables are relatively similar. The broad financial cycle estimate of Schüler et al. (2020) is found to interact closely with U.S. real GDP growth, as well as the U.S. version of the CISS. Short-term and long-term interest rates (implicitly, the term spread) appear to matter as well. The NFCI favored by Adrian et al. (2019) is ranked highly because it is closely related to the U.S.-version of the CISS.

#### Figure F.2: Variable selection for U.S. data

Variables are ranked according to their average check function value in a three-variable Q-VAR. Real quarterly GDP growth (ordered first) and the U.S. CISS (ordered last) remain fixed inputs in the three-variable system. The middle variable is looped over. Check function variables are evaluated at quantiles from 0.1 to 0.9 (decile-by-decile) for the GDP growth and CISS equation only. Estimation sample is 1976Q2 to 2018Q4. Non-stationary time series were de-trended using Hamilton (2018)'s regression filter (q = 8, h = 2) and are marked with a star.



### F.3 Parameter estimates for U.S. data

Figure F.3 reports parameter and standard error estimates for our favorite trivariate specification based on U.S. data. The arrangement of panels in Figure F.3 corresponds to the ordering of variables in (6).

## F.4 Wald test and quantile impulse response functions

Table F.1 reports the outcome of three Wald tests of parameter homogeneity across quantiles. We implement the Wald  $\chi^2$  test as explained in Koenker (2005, Ch. 3.3.2); see also Koenker and Basset (1982). The Wald test strongly rejects the pooling (parameter homogeneity) restrictions implied by a linear specification for the GDP growth and CISS equation for U.S. data. The pooling restrictions are not rejected for the financial cycle equation. The test outcomes are intuitive given the parameter and standard error estimates reported in Figure F.3.

The asymmetries implied by the Wald test outcomes are clearly visible in the shapes of the QIRF; see Figure F.4. As expected, the real GDP response to a shock to the CISS depends markedly on the quantile of interest. The bottom 0.1 quantile of real GDP responds much more strongly than its upper 0.9 quantile. This is not surprising, and in line with Adrian et al. (2020). The response of the CISS to a shock to the financial cycle is highly asymmetric. A shock to the financial cycle does not move the CISS much in most parts of the CISS's distribution. In contrast, the upper 0.9 quantile of the CISS displays a marked negative response in the short term that disappears after approximately one year.

#### Table F.1: Wald test for slope homogeneity for U.S. data

Wald tests statistics. We consider our baseline trivariate QVAR model, estimated decile-by-decile ranging from 0.1 to 0.9; see Figure F.3. The null hypothesis states that the parameter estimates across the p = 9 quantiles are equal to the median estimates. The test statistic is  $\chi^2$ -distributed. The test statistic's degrees-of-freedom (df) is given by the number of right-hand-side variables per equation (excluding the constant, i.e. 3, 4, and 5, respectively) times the number of imposed restrictions (9 - 1 = 8).

	df	test statistic	p-value
real U.S. GDP growth $y_t$	24	66.38	0.00
U.S. financial cycle indicator $c_t$	32	39.25	0.18
U.S. CISS financial stress index $s_t$	40	152.87	0.00

### Figure F.3: Parameter estimates for baseline QVAR model and U.S. data

Parameter estimates from a trivariate QVAR model estimated for p = 9 quantiles from 0.1 to 0.9. Parameter estimates are obtained equation by equation while standard error estimates take cross-equation restrictions into account; see Web Appendix A.1. SE banks are at a 95% confidence level. Estimation sample is 1976Q2 to 2018Q4.



## Figure F.4: Quantile impulse response functions for U.S. data

Impulse response functions implied by the parameter estimates reported in Figure F.3. Impulse response functions are plotted over the next  $1, \ldots, 32$  quarters. Variables are ordered as GDP growth (respective first row), U.S. financial cycle (second row), and U.S. CISS (third row). Estimation sample is 1973Q1 to 2018Q4.



# F.5 Downside risk measures for U.S. data

Figure F.5 plots our estimates for average future growth shortfall (AGS) and longrise (AGL) based on U.S. data. Each estimate is based on full-sample estimates, but is otherwise conditional on variables observed up to time t, covering the next two years t + 1, ..., t + 8.

Time-*t* average future growth shortfall (AGS<sup> $\tau$ </sup><sub>*t*,*t*+1:*t*+8</sub>) and average future growth longrise (AGL<sup> $\tau$ </sup><sub>*t*,*t*+1:*t*+8</sub>), evaluated at  $\tau = 0$  and as reported in Figure F.5, consist of two factors: a tail conditional expectation term, computed as the average of expected GDP growth conditional on negative growth, and the probability of a contraction; see (2) and (4). The top and bottom panel of Figure F.6 plot the first and second factor over time, respectively. Most of the variability in AGS<sup> $\tau$ </sup><sub>*t*,*t*+1:*t*+8</sub> comes from the tail conditional expectation term, with an additional contribution of the contraction probability term in bad times.

#### Figure F.5: Growth shortfall estimates for U.S. data

Growth shortfall estimates based on a three-variable Q-VAR. We estimated a different set of parameters for quantiles ranging from 0.1 to 0.9 (decile-by-decile). Shaded areas indicate NBER recessions. The estimation sample is 1973Q1 to 2018Q4.



#### Figure F.6: AGS and AGL components for U.S. data

Top panel: average future conditional tail expectation; see first factor in (2) and (4). Bottom panel: average future contraction probability; see second factor in (2) and (4). Each estimate is based on p = 20 quantiles ranging from 0.025 to 0.975. We compare these estimates to quarterly annualized real GDP growth (solid line, left scale). Shaded areas indicate US recessions as determined by the CEPR business cycle dating committee. The estimation sample is 1973Q1 to 2018Q4.



### F.6 Model-based stress testing

Figure F.7 reports the time-t conditional forecast of average future real GDP growth  $\bar{y}_{t,t+1:t+4}$  between time t and t + 4 as implied by our trivariate model. The forecast is conditional on a 0.1 (conditional) quantile realization for GDP growth  $y_{t+h}$ , a 0.1 quantile realization of the financial cycle  $c_{t+h}$ , and a 0.8 quantile realization for CISS  $s_{t+h}$ , consecutively for  $h = 1, \ldots, 4$ . The magnitude of these shocks is approximately in line with the eight observed quantile realizations for all variables between 2008Q1 and 2009Q4; see Section 4.3. The stress test is repeated at each  $t = 1, \ldots, T$ , and always based on the same (full sample) parameter estimates. As a result, the figure is informative about the impact of GFC-sized real and financial shocks on real living standards at any time in our sample.

#### Figure F.7: Vulnerability to a GFC stress scenario for U.S. data

Dashed line: U.S. annualized quarterly real GDP growth. Solid line: predicted average annualized quarterly real GDP growth  $\bar{y}_{t,t+1:t+4}$  one year ahead conditional on consecutive 0.1 quantile realizations for GDP growth  $y_t$ , 0.1 quantile realizations of the financial cycle  $c_t$ , and 0.8 quantile realizations for CISS  $s_t$ . Predictions are based on full sample parameter estimates. Estimations sample 1973Q1 – 2018Q4. Horizontal lines refer to 0.1, 0.5, and 0.9 empirical quantiles of  $\bar{y}_{t,t+1:t+4}$ . The vertical line indicates the Lehman Brothers bankruptcy in 2008Q3.



### F.7 Towards a metric for macro-prudential policy stance

Table F.2 summarizes our policy experiment for U.S. data. As in the euro area case, we contrast two counterfactual scenarios. Compared to Table 2 we chose less extreme deciles for the second period H = 7, ..., 12 owing to U.S. data characteristics. Each scenario looks three years into the future, equally split into two periods of H/2 = 6 quarters. The first six quarters are normal times during which the financial cycle could be marginally reduced. The second six quarters refer to a financial crisis during which the CISS takes high values and the financial cycle takes low values.

Figure F.8 plots the utility difference  $\Delta u_t = u_t$  (active) –  $u_t$  (passive) associated with adopting an active macro-prudential policy, where  $u_t$  (·) is given by (17). Again, adopting the active policy is not equally beneficial at all times. The benefits from leaning against the financial cycle are positive during the late 1990s before the bust of the dot-com boom in 2000, and during the mid-2000s before the onset of the global financial crisis in 2007. This is intuitive, as the financial system was buoyant during these times, arguably seeding the respective busts later on. The utility difference  $\Delta u_t$  is mildly correlated with the U.S. financial cycle, suggesting that it is a valuable variable to track to inform macroprudential policy discussions.

#### Table F.2: Passive vs. active macroprudential policy

The top and bottom panels report selected quantiles for GDP growth  $(y_t)$ , financial cycle  $(c_t)$ , and CISS  $(s_t)$  under a passive and active macroprudential policy benchmark, respectively. Multiple quantiles 0.1 - 0.9 mean that the quantile is picked at random. The first six quarters are normal times during which the financial cycle could, in principle, be marginally reduced. The second six quarters refer to a financial crisis during which the CISS takes high values and the financial cycle takes low values. If the financial cycle is actively managed in the first period then it does not not have to contract as much during the crisis.

		first six quarters	second six quarters
		"normal times"	"financial crisis"
passive	$y_t$	0.1 – 0.9	0.1 – 0.9
benchmark	$c_t$	0.7	0.2
	$s_t$	0.1 - 0.9	0.8
active	$y_t$	0.1 - 0.9	0.1 – 0.9
macro-pru	$c_t$	0.6	0.3
policy	$s_t$	0.1 – 0.9	0.8

# Figure F.8: The benefits from active macro-prudential policy for U.S. data The benefit of adopting a less passive macro-prudential policy stance in utility terms, $\Delta u_t = u_t$ (less passive) – $u_t$ (passive); see (17). Parameters are chosen as $\beta = 1$ , $\lambda = 1.5$ , $\tau = 0$ , and H = 12. The difference is based on

 $u_t$  (passive); see (17). Parameters are chosen as  $\beta = 1$ ,  $\lambda = 1.5$ ,  $\tau = 0$ , and H = 12. The difference is based on full sample parameter estimates. Estimation sample is 1973Q1 to 2018Q4. Shaded areas indicate NBER-dated U.S. recessions.



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