

# Housing over the Life Cycle and Across Countries: A Structural Analysis

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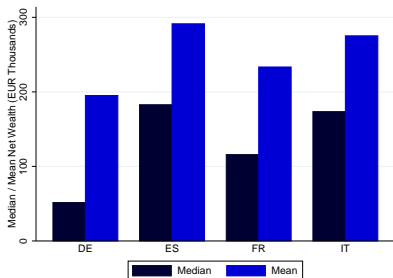
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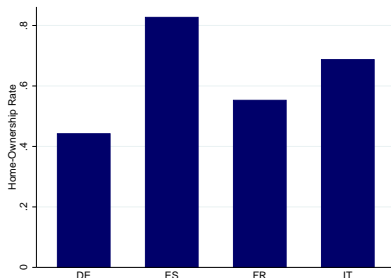
# Motivation

- Striking differences in household wealth across countries
- Driven substantially by housing (real assets  $\approx$  80% of total assets)  
 $\Rightarrow$  **Important to have quantitative model of housing**

Median / mean net wealth

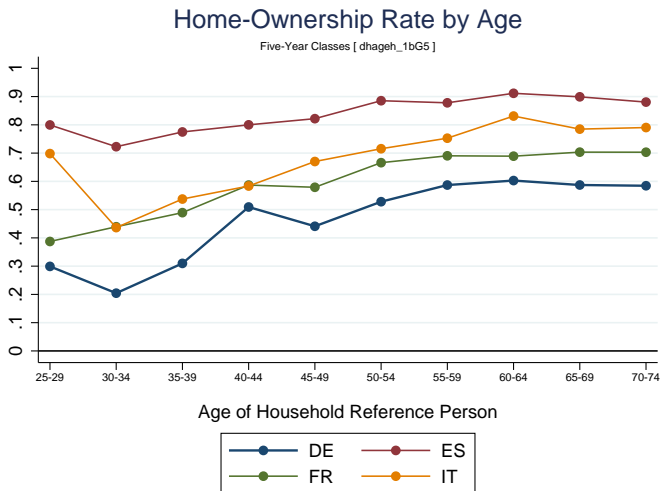


Home-ownership rate



Source: Eurosystem Household Finance and Consumption Survey

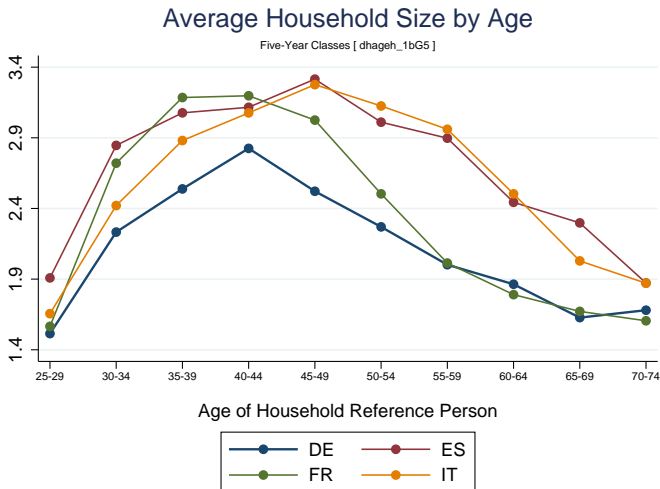
# Home-ownership rate by age



Source: Eurosystem Household Finance and Consumption Survey

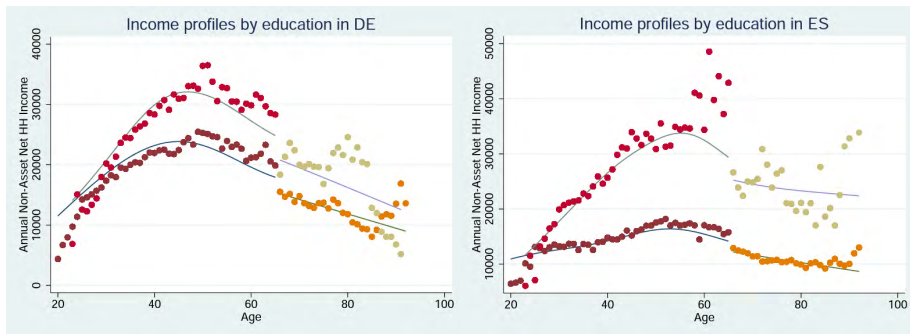
# Household size $N$ : Germany: 2.0 vs Spain: 2.7

$$u(C_t, H_t) = N_t^\gamma (C_t^{1-\omega} H_t^\omega)^{1-\gamma} / (1-\gamma)$$



# Income age profiles

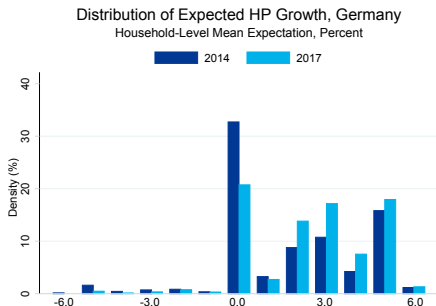
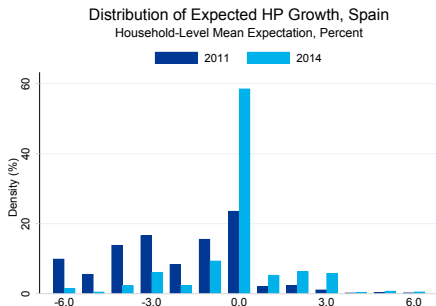
- DE income peaks at around 45 years, much earlier than ES (55)
- Transitory variance twice larger in ES: 0.096 vs 0.048



Source: European Community Household Panel 1994–2001

# Expectations about house prices

- Available at household-level (for some countries)
- Distribution increases in DE, ES



Distribution of one-year ahead expected growth

Source: Encuesta Financiera de las Familias (EFF), Banco de España; Panel on Household Finances (PHF), Deutsche Bundesbank

# Plan of the paper

## Structural life-cycle model

We solve rich model with:

- Discrete house owning–renting choice
- Illiquid housing (adjustment cost)
- Idiosyncratic house price shocks
- Idiosyncratic perm & transitory income shocks
- Collateral constraints

Partial equilibrium



# Literature—Saving / housing across countries

- **Reduced-form:** Chiuri and Jappelli (2003), Calza et al. (2013), ...
- **Structural:** Carroll and Dunn (1997), Gourinchas and Parker (1997), Cagetti (2003), ...
- **Computational—Extensions of Endogenous Grid Method to Discrete Choice:** Carroll (2006), Fella (2014), Druedahl (2017), Iskhakov et al. (2017)
- **Modelling housing over life cycle:**
  - ▶ **US:** Cocco (2004), Cocco et al. (2005), Li and Yao (2007), Yao et al. (2015), Landvoigt (2017), ...
  - ▶ **Other countries:** Kaas et al. (2017), ...
  - ▶ **Cross-country:** Kindermann & Kohls (2017), Hintermaier & Koeniger (2018)

Typically, some features of existing models differ from our setup:  
discrete choice, stochastic HP, income process, ...

# Model—Preferences

- Maximize

$$\mathbf{E}_0 \left\{ \sum_{t=0}^T \beta^t \prod_{s=0}^t \hat{p}_s (\hat{p}_t u(C_t, H_t; N_t) + (1 - \hat{p}_t) B(W_t)) \right\}$$

$\hat{p}$  conditional prob of alive;  $N$  household size;

$W$  net wealth—includes housing (net of selling cost and debt)

- **CRRA utility**, Cobb–Douglas aggregate of  $C$  and  $H$ :

$$u(C_t, H_t) = N_t^\gamma \frac{(C_t^{1-\omega} H_t^\omega)^{1-\gamma}}{1-\gamma}$$

- Warm-glow **bequest**:

$$B(W_t) = L^\gamma \frac{W_t^{1-\gamma}}{1-\gamma}$$

# Model—Housing

- Dual role of housing: asset and durable consumption good

- **Housing is illiquid**

Cost of selling house:  $\phi \times P_t^H \bar{H}_t$

- Collateral constraint

Downpayment at least:  $\delta \times P_t^H H_t$

- House Prices

Geometric random walk:

$$P_t^H = P_{t-1}^H \times \tilde{R}_t^H, \quad \tilde{R}_t^H \sim \mathcal{N}(\mu_H, \sigma_H^2)$$

## Model—Income

- Permanent–transitory household income process:

$$Y_t = P_t \theta_t,$$
$$P_t = \Gamma_t P_{t-1} \psi_t,$$

$\theta$  contains (transitory) unemployment shock

- Deterministic exogenous retirement:

$$Y_t = \tau P_K \text{ for } t > K$$

$\tau$ : retirement replacement rate

### Normalization

- State and choice variables normalized with  $P_t$
- Value function normalized with  $(P_t / (P_t^H)^\omega)^{1-\gamma}$
- Express normalized variables in small letters, eg  $c_t \equiv C_t / P_t$

## Model—Normalized problem

Budget constraints depend on **housing status**

$$v_t(m_t, h_t) = \max_{\{c_t, h_t\}} \left\{ u(c_t, h_t) + \hat{p}_t \beta \mathbf{E}_t \left[ v_{t+1}(m_{t+1}, h_{t+1}) \left( \frac{\Gamma_{t+1} \psi_{t+1}}{(\tilde{R}_{t+1}^H)^\omega} \right)^{1-\gamma} \right] + (1 - \hat{p}_t) B(w_t) \right\}$$

s.t.

$$a_t = \begin{cases} m_t - c_t - \alpha h_t & \text{Renter} \\ m_t - c_t - \lambda h_t & \text{Stayer} \quad h_t = \bar{h}_t \\ w_t - c_t - (1 + \lambda) h_t & \text{Mover} \quad w_t = m_t + (1 - \phi) \bar{h}_t \end{cases}$$

$\alpha$ : rental cost,  $\lambda$ : maintenance cost,  $\phi$ : selling cost,  $\delta$ : downpayment

$m$ : market resources,  $h$ : housing wealth,  $w$ : net wealth

$$m_{t+1} = \frac{R}{\Gamma_{t+1} \psi_{t+1}} a_t + \theta_{t+1}, \quad h_{t+1} = \frac{\tilde{R}_{t+1}^H}{\Gamma_{t+1} \psi_{t+1}} h_t,$$

$$a_t \geq -(1 - \delta) h_t \quad \text{collateral constraint}$$

# Solution: Discrete-choice EGM

- Substantial complication b/c of **discrete owning–renting choice**
- Solve 3 choice-specific problems (renter/stayer/mover) with Endogenous Gridpoints Method (Carroll, 2006)
- Extend EGM to multiple states, discrete choice and constraints:
  - ▶ **Renter R**:  $v^R(m_t)$  – **1D problem**;  $c$  and  $h$  linearly related
  - ▶ **Stayer S**:  $v^S(m_t, \bar{h}_t)$  – **2D problem**; chooses  $c$  for a given  $h = \bar{h}$ , 2 state variables
  - ▶ **Mover M**:  $v^M(m_t + (1 - \phi)h_t)$  – **2D problem**; chooses  $c$  and  $h$  (pays selling cost  $\phi\bar{h}_t$ ), only 1 state at time  $t$  ( $w_t = m_t + (1 - \phi)\bar{h}_t$ )
- **Discrete ownership choice—max over 3 value functions:**

$$v(m_t, h_t) = \max \{ v^R(m_t), v^S(m_t, \bar{h}_t), v^M(m_t + (1 - \phi)\bar{h}_t) \}$$

# Mechanics of the model: Renting vs owning

Benefits / Costs of renters / Homeowners

## Renters

- Costless adjustment of housing  $\Rightarrow h_t = \omega/\alpha(1 - \omega) \times c_t$

## Homeowners

- Capital gains (losses) on housing:  $P_t^H = P_{t-1}^H \times \tilde{R}_t^H$
- Cost of selling house:  $\phi \times \bar{h}_t$
- Subject to **collateral constraint**:  $a_t \geq -(1 - \delta)h_t$

## Cost view

- **Renters**: Young frequently adjust housing — costless if they rent
- **Owners**: Transaction cost generates inertia, prevents from upgrading too frequently;  $h_{t-1}$  is state (for stayer)

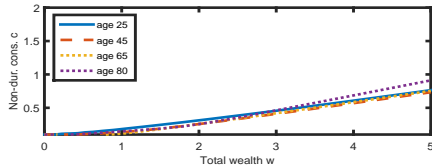
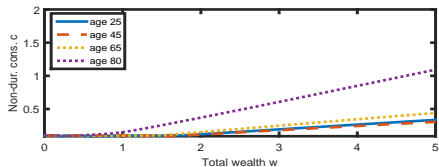
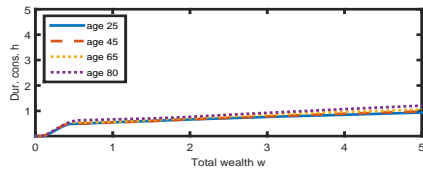
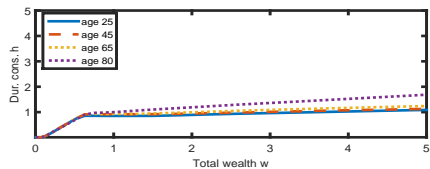
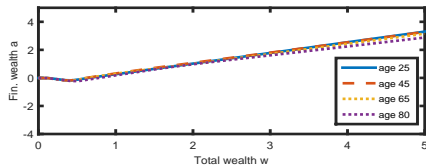
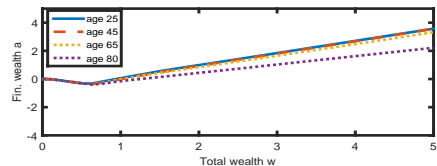
# Calibration

| Parameter                                      | Symbol               | Value         |              |
|--|----------------------|---------------|--------------|
|  |                      | Germany       | Spain        |
| Discount Rate                                  | $\beta$              | 0.94          | 0.94         |
| CRRA   | $\gamma$             | 2             | 2            |
| Bequest Strength                               | $L$                  | <b>3</b>      | <b>7</b>     |
| Weight on Housing                              | $\omega$             | 0.1           | 0.1          |
| Variance of Permanent Income Shock             | $\text{var}(\psi)$   | 0.018         | 0.018        |
| Variance of Transitory Income Shock            | $\text{var}(\theta)$ | <b>0.048</b>  | <b>0.096</b> |
| Unemployment Insurance—Replacement Rate        | $\mu_U$              | 0.50          | 0.40         |
| Income Replacement Ratio After Retirement      | $\tau$               | <b>0.55</b>   | <b>0.80</b>  |
| Mandatory Retirement Period                    | $J$                  | 45            | 45           |
| Maximum Life Cycle Period                      | $T$                  | 65            | 65           |
| Risk-Free Interest Rate                        | $r$                  | 0.01          | 0.03         |
| Mean Growth Rate of House Prices               | $\mu_H$              | <b>-0.001</b> | <b>0.023</b> |
| Variance of Growth Rate of House Prices        | $\sigma_H^2$         | <b>0.010</b>  | <b>0.075</b> |
| Correlation b/w Perm Income and Housing Return | $\rho_{P,H}$         | <b>-0.17</b>  | <b>0.47</b>  |
| Downpayment Requirement                        | $\delta$             | <b>0.40</b>   | <b>0.20</b>  |
| House-Selling Cost                             | $\phi$               | 0.11          | 0.12         |
| Maintenance Cost                               | $\lambda$            | 0.02          | 0.02         |
| Rental Cost                                    | $\alpha$             | <b>0.025</b>  | <b>0.025</b> |



# Wealth profiles of optimal policy functions

Germany versus Spain



# Explaining results: How does calibration matter?

## Germany

### Saving

- Steeper income profile & much less risky HP: HHs get large mortgage
- Stricter downpayment restriction  $\Rightarrow$  binding for most wealth levels
- Weaker bequest motive: Older HHs decumulate wealth faster than in ES

### Durable consumption

- Steeper income profile & less risky HP: HHs buy larger houses

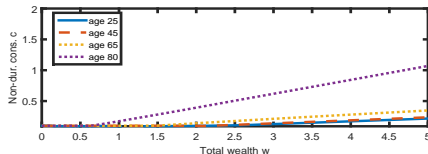
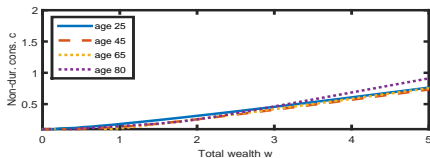
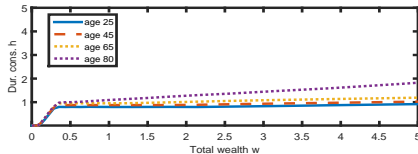
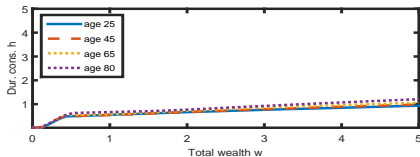
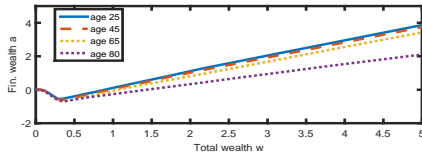
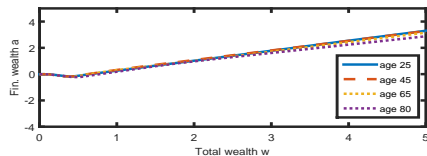
### Nondurable consumption

- Lower consumption
- Only at later age bequest motive comes in

# House price bubble (Spain 1997–2007)

HP growth  $\mu_H$  increases from 2.3% to 7.45%,  $\sigma_H^2$  decreases by 2/3

- Housing gets more attractive
- Indebtedness increases as HHs want to upgrade as much as possible



# Conclusions

## Model generates substantial differences

- Young HHs rent and save for downpayment
- Collateral constraint binds for poor households over entire LC
- HHs sell and upgrade when additional utility exceeds adjustment cost
- HHs with strong bequest motive reduce  $C$  as they age

## Next steps

- Solution & simulation of full model
- Estimation

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## Backup Slides

# Motivation

So far,

- Not enough structural work on cross-country differences in wealth
- Limited quantitative modeling of housing
- Because of data and computational limitations

**But now both data and computational tools available**

# Our contribution

## Computational

- Solve rich model with discrete choice
- Apply extension of **Endogenous Gridpoints Method**
- Eventually, estimate model some parameters (using SMM)

## Empirical

- Calibrate the model carefully using micro data sources
- Interpret **quantitatively** role of key factors for **wealth accumulation across countries**
- Simulate counterfactual scenarios
  - ▶ 'House price bubble'
  - ▶ Tightening of credit constraints
  - ▶ Changes in incomes



# Plan of the paper

## Effects on wealth accumulation

Investigates **quantitatively** role of:

- House prices
- Housing market institutions (LTV ratio, rental protection, taxation of mortgages, ...)
- Expectations
- Demographics
- Income risk
- Bequest motive

... on **wealth accumulation across countries** and life cycle

# Mechanics of the model: Life cycle

- **Young**

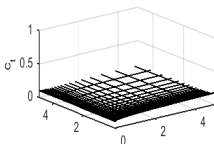
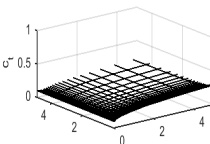
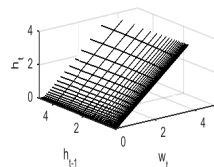
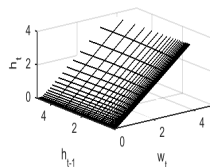
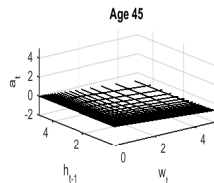
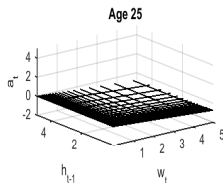
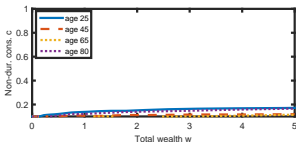
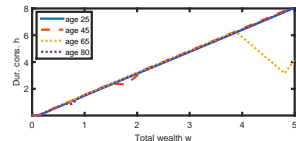
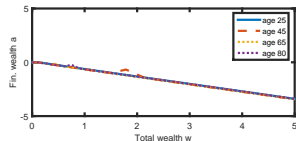
- ▶ Increasing income profile mimics safe asset (as in Cocco et al. (2005))
- ▶ Down payment restriction prevents young from buying
- ▶ Take mortgage to balance **portfolio composition**:  
risky (housing) vs safe assets / future income

- **Old**

- ▶ As HHs age, they reduce leverage and hold positive liquid assets
- ▶ Saving vs consumption depends on strength of bequest motive

# Check: No adjustment cost

Owners upgrade without incurring a fixed cost



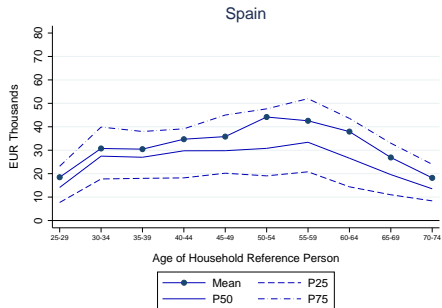
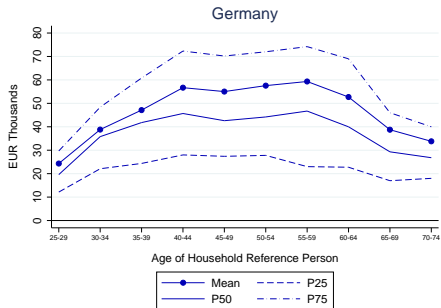
## Explaining counterfactual results: ES house price bubble

- Housing gets more attractive.
- Indebtedness increases as HHs want to upgrade as much as possible.

## Explaining counterfactual results: No adjustment cost

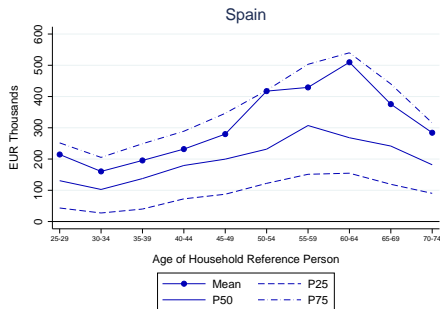
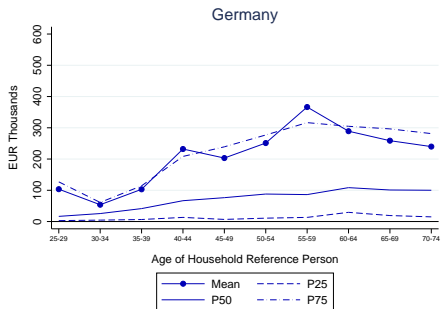
- Homeowners purchase house only for one period.
- Only wealth and income are states; housing revised every period.

# Distribution of Household Income by Age



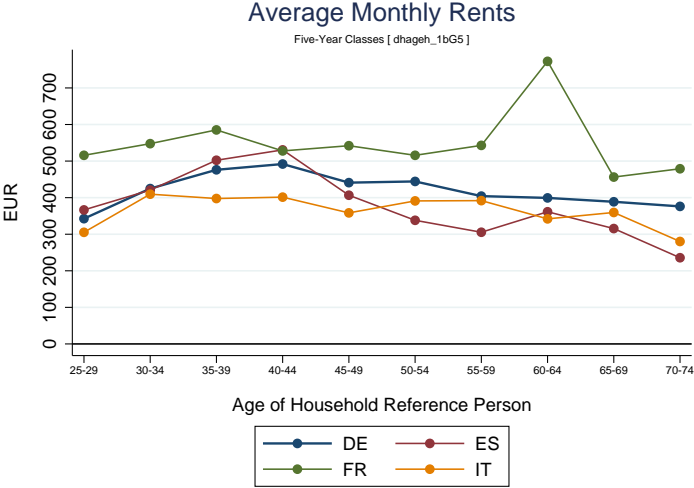
Source: Eurosystem Household Finance and Consumption Survey

# Distribution of Household Net Wealth by Age



Source: Eurosystem Household Finance and Consumption Survey

# Rents

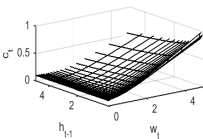
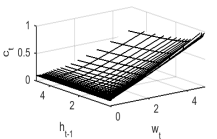
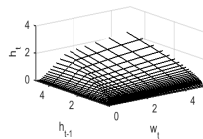
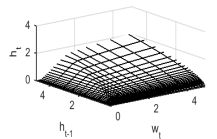
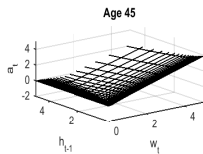
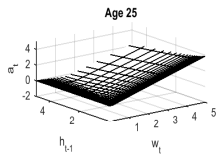
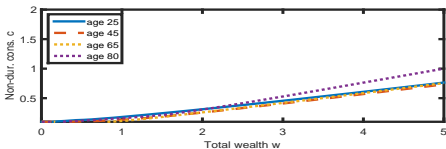
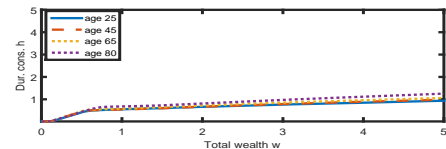
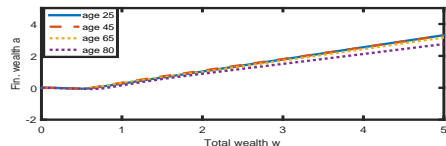


Source: Eurosystem Household Finance and Consumption Survey



# Counterfactual experiment: Tighter constraints

Increase in  $\delta$  from 0.2 to 0.5



## Explaining counterfactual results: Tighter constraints

- Constraints deter HHs from owning too much too quickly.
- HHs consume more non-durable goods.

# Outlook: Structural estimation

- Simulate model using the calibrated values.
- Use moments from the cross-sectional data (homeownership, LTI, LTV).
- Estimate  $\theta \equiv \{\beta, \gamma, L, \omega\}$  by SMM, minimizing distance of model from data:

$$(G_Q - G_{\hat{Q}}(\theta))' D (G_Q - G_{\hat{Q}}(\theta))$$

- Need to recompute model for each estimation and simulation loop.